~ Total mark

10

## Test 1

#### 1 Choose the correct answer from those given :

(3 marks)

1 
$$7 x^2 - 2 x^2 = \cdots$$

(b) 5 
$$x^2$$

$$\bigcirc$$
 9  $x^2$ 

2 The algebraic term 
$$b^3 = \cdots$$

$$(a)$$
 3  $\times$  b  $\times$  b

$$(b)$$
 b + b + b

$$\bigcirc b \times b \times b$$

$$(d)$$
 3 × b

3 If 5 
$$a = 45$$
 and  $b = 1$ , then  $b = \dots$ 

(a) 
$$\frac{1}{45}$$

ⓑ 
$$\frac{1}{9}$$

© 
$$\frac{1}{5}$$

#### Complete the following :

(3 marks)

1 The number that lies half the way between 
$$\frac{1}{2}$$
,  $\frac{3}{4}$  is ......

2 The result of subtracting 
$$-3 \times x^2$$
 from  $5 \times x^2$  is .....

$$\frac{4 y^5}{y^3} + 2 y^2 = \dots$$
 where  $y \neq 0$ 

(2 marks)

$$\frac{3}{7}\times9+\frac{3}{7}\times6-\frac{3}{7}$$

4 Subtract: 
$$5 x^2 + y^2 - 3 x y$$
 from  $3 x y + 5 x^2 + y^2$ 

(2 marks)

Total mark

10

## Test 2

#### 1 Choose the correct answer from those given :

(3 marks)

- 1 If the algebraic expression:  $a X^3 + 5 X^2 + 7 X 9$  is of the second degree, then  $a = \dots$ 
  - (a) 1

(b) 3

- (c)-2
- (d) zero

- 2 a + a + a = .....
  - $\bigcirc$  3  $a^2$
- (b) 3 a
- (c)  $a^3$

- (d)a + 3
- - (a)  $3 x^5$
- (b) 3 X
- © 3  $x^2$
- (d) 3

#### 2 Complete the following:

(3 marks)

- 1 3 X decreases 5 X by .....
- 2 The degree of the absolute term in any algebraic expression is .....
- $\frac{-4}{5} \times \cdots = 1$

3 If 
$$a = \frac{1}{2}$$
,  $b = \frac{2}{5}$ ,  $c = \frac{1}{5}$ 

(2 marks)

- , find the numerical value of the expression :  $(a + b) \div c$
- 4 Add  $3 X^2 + 2 X y 5$  and  $-2 X^2 3 X y + X$

(2 marks)

, then find the numerical value of the result when : X = -1 and y = 2

## Mathematics (Geometry)

## Test

Total mark

#### Choose the correct answer from those given :

(3 marks)

#### 1 In the opposite figure :

 $\overrightarrow{BE}$  bisects  $\angle$  ABC,  $\overrightarrow{BA}$  //  $\overrightarrow{CD}$  and m ( $\angle$  ABE) = 32°

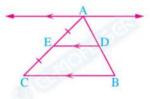
- , then m ( $\angle$  C) = .....
- (a) 32°
- (b) 64°
- (c) 60°
- (d) 80°
- 2 If  $\triangle$  ABC  $\equiv$   $\triangle$  XYZ, m ( $\triangle$  X) + m ( $\triangle$  Y) = 140°, then m ( $\triangle$  C) = .....
  - (a) 180°
- (b) 140°
- (c) 90°
- (d) 40°

#### 3 In the opposite figure :

AD : AB = .....

- (a) 1:1
- C 1:3

- (b) 1:2
- (d) 1:4



#### 2 Complete the following:

(3 marks)

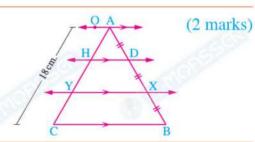
- 1 If two coplanar straight lines are perpendicular to a third one, then the two straight lines are
- 2 The diagonal of the rectangle divides its surface into two ..... triangles.
- 3 Any two right-angled triangles are congruent if .....

#### 🔼 In the opposite figure :

 $\overrightarrow{AO}$  //  $\overrightarrow{HD}$  //  $\overrightarrow{YX}$  //  $\overrightarrow{CB}$ 

AD = DX = XB and AC = 18 cm.

Find the length of :  $\overline{AY}$ 



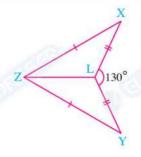
#### In the opposite figure :

YZ = XZ, XL = YL

 $m (\angle XLY) = 130^{\circ}$ 

Prove that :  $\Delta XLZ \equiv \Delta YLZ$ 

, then find :  $m (\angle XLZ)$ 



(2 marks)



### **Test**



#### Choose the correct answer from those given :

(3 marks)

130

1 In the opposite figure :

$$B \in \overline{AC}$$
,  $\overrightarrow{BE} / / \overrightarrow{CD}$ 

and m (
$$\angle$$
 ABE) = 130°

, then m (
$$\angle$$
 C) = .....

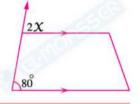
- 2 If  $L_1$  and  $L_2$  are two coplanar straight lines where  $L_1 \cap L_2 = \emptyset$ , then  $L_1$  and  $L_2$  are .....
  - (a) intersecting.
- (b) perpendicular.
- © parallel.
- (d) coincident.

3 In the opposite figure :

What is the value of X?

- (a) 40°
- (c) 80°

- (b) 60°
- (d) 100°



#### 2 Complete the following:

(3 marks)

- 1 If  $\triangle$  ABC  $\equiv$   $\triangle$  XYZ, then AB XY = .....
- 2 If  $\triangle$  CDE  $\equiv$   $\triangle$  LMN, the perimeter of  $\triangle$  CDE = 12 cm., LM = 4 cm., MN = 5 cm. , then LN = .....
- 3 The straight line which is perpendicular to one of two parallel straight lines is ..... to the other straight line in the plane.

#### 🚺 In the opposite figure :

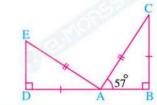
(2 marks)

$$BC = AD$$
,  $AC = AE$ 

$$, m (\angle B) = m (\angle D) = 90^{\circ}$$

and m (
$$\angle$$
 CAB) = 57°

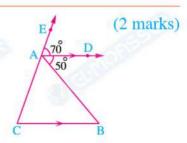
Find the measures of the unknown angles in  $\triangle$  ADE



#### In the opposite figure :

, m (
$$\angle$$
 DAE) = 70° and m ( $\angle$  DAB) = 50°

Find the measures of the angles of the triangle ABC





(Algebra and Statistics)

#### **Answers of Test**

1

$$\frac{5}{8}$$
 or 0.625

$$28x^{2}$$

$$36 y^2$$

$$\frac{3}{7} \times [9+6-1] = \frac{3}{7} \times \cancel{14} = 6$$

$$\frac{3 \times y + 5 \times^{2} + y^{2}}{-3 \times y + 5 \times^{2} + y^{2}} = \frac{-3 \times y + 5 \times^{2} + y^{2}}{6 \times y}$$

#### **Answers of Test**



$$\frac{-5}{4}$$
 or  $-1\frac{1}{4}$ 

$$\frac{1}{\left(\frac{1}{2} + \frac{2}{5}\right) \div \frac{1}{5} = \left(\frac{5}{10} + \frac{4}{10}\right) \div \frac{1}{5} = \frac{9}{10} \div \frac{1}{5} = \frac{9}{10} \times \frac{\frac{1}{5}}{1} = \frac{9}{2} }$$

$$3 x^{2} + 2 x y - 5$$

$$-2 x^{2} - 3 x y + x$$
The sum =  $x^{2} - x y + x - 5$ 

, the numerical value = 
$$(-1)^2 - (-1) \times 2 + (-1) - 5 = 1 + 2 - 1 - 5 = -3$$

# **Answers of Mathematics**

(Geometry)

#### **Answers of Test**





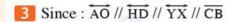
2 d

3 (b)

2 1 parallel

2 congruent

3 the hypotenuse and a side of one triangle are congruent to the corresponding parts of the other triangle.

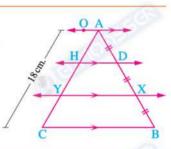


, AB and AC are two transversals to them.

$$, AD = DX = XB$$

, then : AH = HY = YC = 
$$\frac{18}{3}$$
 = 6 cm.

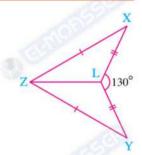
, then : 
$$AY = 12 \text{ cm}$$
.



 $\Delta XLZ \equiv \Delta YLZ$ 

because 
$$\begin{cases} XL = YL \\ XZ = YZ \\ \overline{LZ} \text{ is a common side} \end{cases}$$

, then : m (
$$\angle$$
 XLZ) = m ( $\angle$  YLZ) =  $\frac{360^{\circ} - 130^{\circ}}{2}$  = 115°



**Answers of Test** 

1 1 C

2 (c)

3 (a)

2 1 zero

2 3 cm.

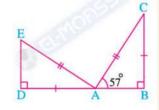
3 perpendicular

3 From  $\triangle$  ABC : m ( $\angle$  ACB) = 180° - (90° + 57°) = 33°

 $\Delta$  ABC  $\equiv$   $\Delta$  EDA (Hypotenuse and one side).

, m (
$$\angle$$
 E) = m ( $\angle$  BAC) = 57°

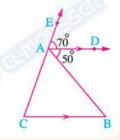
, m (
$$\angle$$
 EAD) = m ( $\angle$  ACB) = 33°



4 m ( $\angle$  B) = m ( $\angle$  DAB) = 50° (alternate angles)

$$m (\angle C) = m (\angle EAD) = 70^{\circ} (corresponding angles)$$

$$m (\angle BAC) = 180^{\circ} - (50^{\circ} + 70^{\circ}) = 60^{\circ}$$



# Sheet (4) Mujtiplying and Dividing Rational Numbers

### Properties of the Multiplication operation in Q:

#### (1) Closure property:

The product of any two rational numbers is a rational number. i.e.: Q is closed under multiplication operation.

#### (2) Commutative property:

If a and b are two rational numbers, then  $a \times b = b \times a$ 

#### (3) Associative property:

If a, b and c are three rational numbers, then  $(a \times b) \times c = a \times (b \times c)$ 

#### (4) Multiplicative identity:

One is the multiplicative identity (multiplicative neutral element). If a is a rational number, then  $1 \times a = a \times 1 = a$ 

#### (5) Multiplicative inverse (reciprocal of the number):

For any rational number  $\frac{a}{b}$  except zero there is a multiplicative inverse that is the number  $\frac{b}{a}$ , where:  $\frac{a}{b} \times \frac{b}{a} = 1$ 

- Zero has no multiplicative inverse because  $\frac{1}{zero}$  is undefined.
- Multiplying any rational number by zero equals to zero.

#### (6) Distribution property:

If a, b and c are three rational numbers, then  $a \times (b + c) = a \times b + a \times c$  $a \times (b - c) = a \times b - a \times c$ 

#### **Properties of operations:**

operation Property	Addition	Subtraction	Multiplication	Division
Closure	✓	✓	✓	*
Commutative	✓	*	✓	*
Associative	✓	*	✓	*
Identity element	<b>√</b> (0)	*	<b>√</b> (1)	*
Inverse	✓	*	✓except (0)	×



#### [1] Complete:

- (1) The multiplicative identity element in Q is
- (2) The multiplicative inverse of  $\frac{3}{7}$  is
- (3) The multiplicative inverse of  $\frac{-2}{3}$  is
- (4) The multiplicative inverse of -6 is
- (5) The multiplicative inverse of  $3\frac{1}{2}$  is
- (6) The multiplicative inverse of 0.5 is
- (7) The multiplicative inverse of 1 is
- (8) The multiplicative inverse of -1 is
- (9) The multiplicative inverse of  $\left(-\frac{3}{5}\right)^{zero}$  is \_\_\_\_\_
- (10) The multiplicative inverse of  $\left|-\frac{3}{5}\right|$  is
- (11) The rational number that has no multiplicative inverse is
- (12) The rational number  $\frac{a-1}{5}$  has a multiplicative inverse if  $a \neq \dots$



#### [2] Put ( $\checkmark$ ) for the correct statement and ( $\times$ ) for the incorrect one:

- (1) Every rational number has a multiplicative inverse. ( )
- (2) The multiplicative inverse of a rational number is an integer. ( )
- (3) The multiplicative inverse of the number  $\frac{0}{7}$  is  $\frac{7}{0}$ .
- (4) The multiplicative inverse of the number  $2\frac{1}{5}$  is  $5\frac{1}{4}$ .
- (5) The multiplicative inverse of the number  $\left(\frac{2}{7} + \frac{3}{5}\right)$  is  $\frac{35}{31}$ .



#### [3] Complete:

The number	The additive inverse	The multiplicative inverse
3 7		
<u>-4</u> 9		
-6		
0.5		
3 1/2		
$\left(\frac{-3}{8}\right)^{zero}$		
$\left -\frac{3}{7}\right $		
1		
-1		
0		

#### [4] Complete:

(1) 
$$\frac{3}{2} \times \left(\frac{-4}{5}\right) = \frac{-4}{5} \times \dots$$
 property

(2) 
$$\frac{2}{3} \times \frac{3}{2} = \dots$$
 property

(3) 
$$7 \times \frac{\cdots}{7} = 1$$
 property

$$(4) \quad -\frac{4}{5} \times \dots = -\frac{4}{5}$$
 property

(5) 
$$-\frac{4}{11} \times \dots = 1$$
 property

(6) 
$$2\frac{3}{5} \times \dots = 1$$
 property

(9) 
$$\frac{2}{3}\left(2+\frac{1}{2}\right) = \frac{2}{3} \times 2 + ... \times ...$$
 property

(10) 
$$\frac{3}{9} = \frac{2}{3} \times \frac{...}{8}$$

(11) If 
$$\frac{x}{y} = \frac{2}{3}$$
 then,  $\frac{3x}{2y} = \dots$ 

(12) If 
$$\frac{a}{b} = 70$$
 then  $\frac{a}{2b} = .....$ 



#### [5] Find out the result of each of the following in the simplest form:

(1) 
$$\frac{3}{5} \times \frac{2}{7} = \dots$$

(2) 
$$\frac{-1}{2} \times \frac{2}{3} = \dots$$

$$(3) \quad -\frac{3}{8} \times \left(-\frac{5}{3}\right) = \ldots$$

$$(4) \quad \frac{2}{6} \times \left(-\frac{3}{4}\right) = \ldots$$

$$(5) \quad \left(-\frac{2}{3}\right) \times \frac{5}{8} = \dots$$

$$(6) \quad \frac{4}{5} \times \left(-\frac{5}{7}\right) = \ldots$$

(8) 
$$\frac{1}{2} \times |-12| = \dots$$



### [6] Find out the result of each of the following in the simplest form:

(1) 
$$\frac{4}{5} \div \frac{3}{7} = \dots$$

(2) 
$$-\frac{1}{6} \div \frac{5}{2} = \dots$$

(3) 
$$\frac{-4}{11} \div \left(\frac{-4}{11}\right) = \dots$$

$$(4) \quad \frac{5}{27} \div \frac{1}{9} = \dots$$

$$(5) \quad \frac{5}{6} \div \left(\frac{-15}{2}\right) = \ldots$$

(6) 
$$\frac{-5}{8} \div \frac{5}{8} = \dots$$

(7) zero 
$$\div \frac{3}{5} = \dots$$

(8) 
$$1 \div \frac{7}{5} = \dots$$



#### [7] Find out the result of each of the following in the simplest form:

(1) 
$$3\frac{1}{2} \times (-4) = \dots$$

$$(2) 1\frac{1}{2} \times \left(\frac{-3}{2}\right) = \ldots$$

(3) 
$$\left(-4\frac{2}{7}\right) \times \left(-5\frac{1}{6}\right) = \dots$$
 (4)  $3\frac{1}{8} \times \left(-4\frac{1}{5}\right) = \dots$ 

(4) 
$$3\frac{1}{8} \times \left(-4\frac{1}{5}\right) = \dots$$

$$(5) \quad \left(-1\frac{1}{2}\right) \times \left|-\frac{5}{3}\right| = \ldots$$

(6) 
$$0.6 \times 1\frac{1}{3} = \dots$$



#### [8] Find out the result of each of the following in the simplest form:

(1) 
$$-2\frac{1}{5} \div \frac{11}{5} = \dots$$

$$(2) -7\frac{5}{6} \div \frac{47}{100} = \dots$$

$$(3) -4\frac{2}{7} \div 1\frac{1}{14} = \dots$$

(4) 
$$-4\frac{1}{3} \div \left(-3\frac{1}{4}\right) = \dots$$

(5) 
$$-2\frac{3}{4} \div \left(-3\frac{1}{8}\right) = \dots$$

(6) 
$$6\frac{1}{4} \div (-15) = \dots$$

[9] Using the distribution property, find out the result of each of the following in the simplest form:

(1) 
$$\frac{5}{12} \times 3 + \frac{5}{12} \times 9 =$$

(2) 
$$\frac{4}{9} \times 11 + \frac{4}{9} \times 16 =$$

(3) 
$$\frac{6}{37} \times 7 + \frac{6}{37} \times 5 + \frac{6}{37} \times (-11) = \dots$$

(4) 
$$\frac{7}{12} \times 5 + \frac{7}{12} \times 9 - \frac{7}{12} \times 2 =$$

(5) 
$$\frac{7}{13} \times 6 + \frac{7}{13} \times 8 - \frac{7}{13} =$$

(6) 
$$\left(\frac{-3}{7}\right) \times 8 + 5 \times \left(\frac{-3}{7}\right) + \left(\frac{-3}{7}\right) = \dots$$



[10] Find the result in the simplest form:

(1) 
$$\left(\frac{3}{8} + \frac{5}{8}\right) \div \frac{5}{8} = \dots$$
 (2)  $\frac{3}{4} \times \left(\frac{1}{2} - \frac{1}{3}\right) = \dots$ 

(2) 
$$\frac{3}{4} \times \left(\frac{1}{2} - \frac{1}{3}\right) = \dots$$

(3) 
$$\left(\frac{-18}{5} \div \frac{9}{35}\right) \times \left(\frac{-3}{7}\right) = \dots$$
 (4)  $-4\frac{1}{3} \div \left(-3\frac{1}{4}\right) = \dots$ 

(4) 
$$-4\frac{1}{3} \div \left(-3\frac{1}{4}\right) = \dots$$

(5) 
$$\left[\frac{-12}{25} \times \left(-\frac{5}{7}\right)\right] \div \left(\frac{-9}{14}\right) = \dots$$
 (6)  $\left[\left(-1\frac{2}{3}\right) \times 4\frac{2}{3}\right] \div 6\frac{1}{9} = \dots$ 

(6) 
$$\left[\left(-1\frac{2}{3}\right) \times 4\frac{2}{3}\right] \div 6\frac{1}{9} = \ldots$$



[11] Find the value of (n) in each of the following:

(1) 
$$\frac{-7}{3} \times \frac{-3}{7} = n$$

(2) 
$$n \times \frac{17}{3} = 1$$

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$\frac{-7}{3} \times n = 0$	)
	_,

$$(4) \qquad \frac{5}{7} \times n = \frac{5}{7}$$

(5) 
$$n \times \left\lceil \frac{1}{2} + \left( \frac{-3}{5} \right) \right\rceil = n \times \frac{1}{2} + 5 \times \left( \frac{-3}{5} \right)$$



[12] If a = 2,  $b = \frac{1}{2}$  and  $c = \frac{3}{2}$ , find in the simplest form the value of:  $(a - b) \div c$ 



[13] If  $x = \frac{1}{3}$ ,  $y = \frac{3}{4}$  and z = -3, find in the simplest form the numerical value of each of the following:

$$(1) xyz =$$

$$(2) xy+zy=$$



[14] If  $x = \frac{3}{4}$  and  $y = \frac{-5}{3}$ , find in the simplest form the value of the expression:

$$\frac{x-y}{x+y} =$$



# Sheet (5) Applications on Rational Numbers

- The distance between two numbers 2 and 5 is:
  |2-5| = |5-2| = 3 length units
- The distance between two numbers -2 and 3 is:
   |-2-3| = |3+2| = 5 length units
- From the side of the smallest number: s + f(g s)
- From the side of the greatest number: g f (g s)



Ex (1): Find the rational number lying at the middle of the way between 3 and 7.

The number = 
$$s + f(g - s) =$$

Or

The number = 
$$g - f(g - s) =$$

Ex (2): Find the rational number lying at the half-way between  $\frac{3}{7}$  and  $\frac{3}{7}$ .

The number = 
$$s + f(g - s) =$$

Ex (3): Find the rational number lying at one third of the way between 2 and 8.

From the side of the smaller number = s + f(g - s) =From the side of the greatest number = g - f(g - s) =



# [1] Find the rational number in the middle of the way (half-way) between:



(2) 
$$\frac{-3}{4}$$
 and  $\frac{3}{4}$ 

(3) 
$$\frac{1}{2}$$
 and  $\frac{7}{8}$ 

(4) 
$$\frac{-11}{4}$$
 and  $\frac{-13}{35}$ 



#### [2] Find the rational number lying at:

- (1) One fourth of the way between  $\frac{5}{7}$  and  $\frac{-3}{7}$  from the side of the smaller number.
- (2) One third of the way between  $\frac{-3}{5}$  and  $\frac{-4}{5}$  from the side of the greater number.
- (3) One third of the way between  $\frac{4}{7}$  and  $1\frac{3}{4}$  from the side of the smaller number.
- (4) One fifth of the way between  $\frac{-2}{3}$  and  $\frac{-3}{5}$  from the side of the smaller number.

#### [3] Choose the correct answer:

(1) If 
$$a \times \frac{b}{2} = \frac{a}{2}$$
,  $a \neq 0$ , then  $b = \frac{a}{2}$   
(a)  $\frac{a}{2}$  (b) 0 (c) a (d) 1 (e) -a

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- (2) If  $\frac{x}{3} 4 = 6$ , then  $\frac{x}{3} + \frac{2}{3} = \frac{1}{3}$ 
  - (a) 1

- (b) x (c)  $\frac{32}{3}$  (d) 10 (e)  $\frac{2x}{9}$
- (3) If  $\frac{x}{y} = 1$ , then  $2x 2y = \frac{1}{2}$ 
  - (a) 4

- (b) 2 (c) 1 (d) 0 (e)  $\frac{1}{2}$
- (4) If  $x + \frac{2}{x} = 5 + \frac{2}{5}$ , then  $x = \frac{1}{5}$ 

  - (a)  $\frac{1}{5}$  (b)  $\frac{4}{5}$  (c) 1 (d)  $\frac{5}{2}$  (e) 5

- (5) If 5a = 45 and ba = 1, then  $b = (a) \frac{1}{45}$  (b)  $\frac{1}{9}$  (c)  $\frac{1}{5}$  (d) 5 (e) 9

- (6) The number  $\frac{x-3}{x-5} \in Q$  if  $x \neq \dots$ 

  - (a) 3 (b) -3 (c) 5 (d) -5 (e) 15



[4] Find three rational numbers lying between  $\frac{3}{2}$  and  $\frac{3}{4}$ , such that one of them is an integer.

### Sheet (6) Algebraic Expressions

### The perimeter and the area of some shapes

#### [1] The square:

$$P = S \times 4 = 4 S$$
 (coeff. = 4 and degree = 1st)

#### [2] Rectangle:

$$P = (\ell + \omega) \times 2 = 2(\ell + \omega)$$

$$A = \ell \times \omega = \ell \omega$$
 (coeff. = 1 and degree =  $2^{nd}$ )

#### [3] Parallelogram:

$$P = (x + y) \times 2 = 2(x + y)$$

$$A = b \times h = b h$$

#### [4] Rhombus:

#### [5] Triangle:

- P = the sum of all side lengths
- Perimeter of equilateral triangle = 3 S

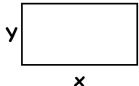
$$A = \frac{1}{2}bh$$

If we denote one pound by x, if we have 3 pounds  $x + x + x = 3 \times (coeff. = 3 \text{ and degree} = 1^{st})$ 

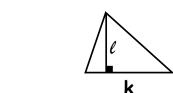
- The algebraic term is formed from the product of two or more factors.
- The degree of the algebraic term is the sum of the indices of the algebraic factors in this term.
- Any number is an algebraic term of zero degree.
- The algebraic term has no algebraic factors is called the absolute term.
- The algebraic expression consists of an algebraic term (monomial) or more.
- The degree of the algebraic expression is the highest degree of its terms.



[1] Write the algebraic term that represent the area of each shape:



a





5

#### [2] Complete the table:

Algebraic term	2 a b²	7 a b <sup>3</sup> c	-8 x <sup>2</sup> b	3	(-2) <sup>3</sup>	$\frac{1}{2}x^3y\ z^2$
Coefficient						
Degree						



#### [3] Complete the table:

The Algebraic expression	No. of terms	Name	Degree
-3 α⁵ b		MONOMIAL	
$3x^2 + y$		BINOMIAL	
$5x^3 - 7x + 4$		TRINOMIAL	
$2a^2 b + 3a b^2 - a^2 b^2$		TRINOMIAL	
$x^2 y^2 - 3x y^4$		BINOMIAL	
$a^2$ b - 3a $b^3$ + 2 $a^3$ $b^2$ + $b^4$		QUADRILATERAL	



#### [4] Complete:

(1)	The coefficient of alc	pebraic term $3 x^2$	v isand its dear	ee is
<b>.</b>	1110 000111010111 01 010	JODI GIO I OI III O A	y is aria i is acqi	OO 10

(2)	The coefficient of algebraic term	$\frac{1}{2}x^3yz^2$	is	and its
degr	ee is			

(3) The degree of the absolute term in an algebraic expression is ......

	(4)	The algebraic	expression	$5x^2 + 3$	is of	the	deare	e
١		inc algoriale	CXPI C331011		13 0 1	1110	acqı c	•



#### [5] Choose the correct answer:

- (1) The degree of the algebraic term  $2x^3y^2$  is \_\_\_\_\_\_ (a) second (b) third (c) fourth (d) fifth
- (2) The coefficient of the algebraic term  $3xy^3z^4$  is \_\_\_\_\_\_ (a) 2 (b) 3 (c) 6 (d) 7

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(3) The degree of the algebraic expression  $3x^2 + 3x^4$  equals to the degree of the algebraic expression ......

(a)  $5xy+3y^2z$ 

(b)  $2x^2y^2 + 3x^2y$  (c)  $2xy + 3x^4z$  (d)  $5a^2b + 4ab^2$ 

(4) The number of terms of the algebraic expression  $3x^2+5xy+6$  is ...... (a) 1 (b) 2 (c) 3 (d) 4

(5) The operation is unclosed in the set of rational numbers.

(a) addition (b) subtraction (c) division (d) multiplication

(6) If the degree of the algebraic term  $2a^3b^n$  is ninth, then  $n = 2a^3b^n$  (a) 8 (b) 6 (c) 2 (d) 9



[6] Arrange the terms of the following algebraic expressions according to the descending order of the indices of a:

(1)  $5a + a^2 - 7 + a^3 =$ 

(2)  $2 a^2 b^2 + 5 b a^3 - 3 b^3 a =$ 



[7] Arrange the terms of the following algebraic expressions according to the ascending order of the indices of x:

(1)  $5x + x^2 - 7 + x^3 =$ 

(2)  $2 x^2 y^2 + 5 y x^3 - 3 y^3 x =$ 



#### Sheet (7) Ljke Algebraic Terms

The algebraic terms are said to be like if they having the same symbols and the same degree. Such as:

Like terms	Unlike terms
$\sim$ 2a , a and -5a . $\sim$ 2x <sup>2</sup> y , 4yx <sup>2</sup> and $-\frac{1}{2}x^2y$	$2x$ , $-3x^2$ and $7x^3$ $4x^2$ , $5xy$ and $y^2$

#### [1] Put $(\checkmark)$ for the correct statement and (\*) for the incorrect one:

- (1) The two algebraic terms  $x^2$  and 2x are like terms. ( )
- (2) The two algebraic terms 3 a  $b^2$  and a  $b^2$  are like terms. ( )
- (3) The two algebraic terms  $7x^2$  and  $2x^7$  are like terms. ( )
- (4) The two algebraic terms 3  $a^2$   $b^3$  and -2  $b^3$   $a^2$  are like terms. ( )
- (5)  $2 a + 3 a = 5 a^2$  ( )
- (6)  $7 x^2 2 x^2 = 5 x^2$
- (7)  $8y^2 5y = 3y$  ( )
- (8) 3ab-3ba=zero ( )

### [2] Find the result of each of the following:

- (1)  $3 \times + \times =$  (2) 7 y y =
- (3)  $3 \times + 2 \times =$  (4) 5 y 3 y =
- (5) 4z-11z= (6) -7x-2x=
- (7) 2 a + 3 a 4 a = (8)  $3 a^2 + 5 a^2 =$
- (9)  $\frac{5x}{4} + \frac{3x}{4} =$  (10)  $\frac{3x}{5} \frac{x}{5} =$

#### [3] Answer each of the following:

(1) Subtract y<sup>2</sup> from -3y<sup>2</sup>

(2) Subtract -6x<sup>2</sup>y from 9x<sup>2</sup>y

(3) What is the increase -2x of -5x?

(4) What is the increase  $3a^2b$  of  $a^2b$ ?

(5) What is the decrease -3ab of 2ab?

(6) What is the decrease  $6x^2y$  of  $-7x^2y$ ?

#### [4] Complete:

(1) The result of subtracting 3a from 7a is

(2) The result of subtracting  $3x^2$  from  $-5x^2$  is

(3) The result of subtracting 7y³ from zero is

(4) The result of subtracting -3a from 2a is

(5) 5a increases 3a by

(6) 7x increases -3x by

(7) 4x decreases 7x by

(8) 5x decreases 3x by

(9) 2x decreases 4x by while 2x increases 4x by

(10)  $+ 2a^2 = 7a^2$ 

(11)  $3x^2$  - =  $x^2$ 

(12)  $2m^2 +$  = zero

(13)  $5 a^2 b - \dots = 7 a^2 b$ 

(14) If 4x - y = 11 and y = 3x, then x =

# [5] If the sum of two terms is 12 x2 y one of them is 4 x2 y. Find the other term.

#### [6] Reduce to the simplest form:

(3) 
$$3x - 5y - x + 2y =$$



#### [7] Reduce each of the following algebraic expressions:

(1) 
$$5x + 4 - 3x^2 - 6x - 7x^2 - 1 =$$

(2) 
$$6 x^2 y - 3 x y^2 + 2 x y^2 - 5 x^2 y + 2 x^2 y^2 =$$

(3) 
$$a^2 + 4a - 5 + 3a^2 - 6a + 1 =$$

(4) 
$$5 x^2 - 2 x + 8 - 7 x - 3 + x^2 =$$



# Sheet (8) Adding and Subtracting Expressions

#### [1] Find the sum of each of the following:

(1)  $3 \times -2 y + 5$  and x + 2 y - 2

(2)  $3n^2 + 5n - 6$  and  $-n^2 - 3n + 3$ 

(3)  $3\ell - 4m + 5n$  and  $4m - 5n - \ell$ 

(4)	$3a^3-2a^2b+b^3$	and	$a^3+4a^2b-b^3$
•			

.....

### [2] Find the sum:

(1) 3a + 2b - 5 , 2a - 7b + 4 , 5b - 4a + 3

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(2	) 3x	+	3y	_	Z
<b>\</b> -		•	$\sim$ $_{7}$		_

$$3x + 3z - 2y$$
  $x + 2y + z$ 

$$x + 2y + z$$

(3) 
$$5x^2 - 3x + 9$$
 ,  $x^2 + 2x - 5$  ,  $x^2 - 3 - 6x$ 

(4)  $3x - 4x^2 + 2$  ,  $x^2 + x - 5$  ,  $3 + 3x^2 - 4x$ 



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[3] Subtract:





[4] What is the increase of:

(1)





#### [5] What is the decrease of:

(1) 2a + 3b + 16a + 16

[6] Subtract x + x2 - 5 from 2x2 + x - 3, then find the numerical value of the result when x = 6

#### 

#### [1] Multiply:

$$(1) \quad \mathbf{5}x \times \mathbf{3}y \quad = \quad$$

$$(2) \quad (-3a) \times 7c \qquad = \qquad \qquad$$

$$(3) \quad 2x \times (-3x) \quad = \quad$$

(4) 
$$(-8y^5) \times (-7y^4)$$
 = \_\_\_\_\_\_

$$(5) \quad 2xy \times \left(-3x^2\right) \quad = \quad \dots$$

(6) 
$$5x^3y^4 \times 2xy^2 =$$

$$(7) 5ab^2 \times \left(-2a^2b\right) =$$

(8) 
$$ab \times (-3a) \times (-2b) =$$

$$(9) 2x3 \times (-3x2) \times (-5x4) =$$

$$(10) \quad (-2x) \times 4x \qquad = \qquad \qquad$$

[2] If the symbols represent non-zero integers, find the quotient of each of the following:

(1) 
$$6a \div 2 =$$

(2) 
$$10c \div 2c =$$

(3) 
$$12x \div (-x) =$$

(4) 
$$(-14x^2) \div 7x =$$

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(5) 
$$\left(-25a^{6}\right) \div \left(-5a^{2}\right) =$$

(6) 
$$24c^5 \div (-24c^5)$$
 =

(7) 
$$9x^5y^4 \div 6x^3y = \dots$$

(8) 
$$\left(-32a^3b^6\right) \div \left(-4a^3b^2\right) =$$

(9) 
$$8m^4n^3 \div (-4m n^2) =$$

#### [3] Simplify:

(1) 
$$\frac{2}{3}t^4 \times \frac{3}{2}t^4 = \dots$$

(2) 
$$\frac{2}{7}a^2 \times 21a^5 =$$

(3) 
$$\frac{6x^4y^2}{7} \times \frac{28x \ y^3}{3} = \dots$$

(4) 
$$3x^3 \times \frac{1}{6}x^2 =$$

#### [4] Choose the correct answer:

(1) 
$$3a^4b \times 5a^2b^2 \times 2a^3 = \dots$$

(a) 
$$60a^{11}b^3$$

(b) 
$$30a^{10}b^2$$

(a) 
$$60a^{11}b^3$$
 (b)  $30a^{10}b^2$  (c)  $150a^{10}b^3$  (d)  $30a^9b^3$ 

(d) 
$$30a^9b^3$$

(2) 
$$(-3x^2y)^2 \times 2xy = \dots$$

(a) 
$$-18x^5y^3$$
 (b)  $18x^5y^3$  (c)  $6x^3y^2$  (d)  $9x^2y^2$ 

(b) 
$$18x^5y^3$$

(c) 
$$6x^3y^2$$

(d) 
$$9x^2y^2$$

(3) 
$$\left(-6x^3y^2\right) \div 3x^2y = \dots$$

(a) 
$$-2x^2y$$
 (b)  $2xy$ 

(c) 
$$-2xy$$

(c) 
$$-2xy$$
 (d)  $-2x^2y^2$ 

#### Mathematics 1<sup>st</sup> Prep 1<sup>st</sup> term

- - (a)  $4b^2$
- (b)  $2b^3$
- (c)  $4b^3$
- (d)  $8b^3$
- (5) If the area of a rectangle is  $24x^3$  cm<sup>2</sup> and its length is  $8x^2$  cm, then its width is
  - (a) 3x
- **(b)**  $3x^2$
- (c) 4x
- (d)  $4x^5$



#### [5] Complete:

(1) 
$$9a^5 = 3a \times ....$$

(2) 
$$36a^5b^8 = 12a^3b^2 \times \dots$$

(3) 
$$-4c^3d^3 = 2c d^2 \times \dots$$

(4) 
$$81l^4 \div \ldots = 27l^3$$

(5) ..... ÷ 
$$6a^2 = -4a^4$$

(6) 
$$36a^7b^4 = \dots \times 9a^7b$$



# Sheet (10) [[Uliplying a monomial by an algebraic expression

#### [1] Find the following products:

$$(1) \qquad a(a+1) \qquad = \qquad \dots$$

(2) 
$$a(a-2) =$$

(3) 
$$3x(7y - 4z) =$$

(4) 
$$-3(y+3) =$$

$$(5) -2c(7-3c) =$$

(6) 
$$2x(3x^2 + 4y^2) =$$

(7) 
$$-5x(2x + y - 3z)$$
 =

(8) 
$$3xy(2x^2 - 5x^2y - 4y^2) =$$

(9) 
$$l m^2 (l^2 - 3m l - 4m^2) =$$

(10) 
$$\frac{1}{3}x^2(6x^2 - 9xy - 3y^2)$$
 =



#### [2] Put in the simplest form:

(1) 
$$3a(a-b) + 4a(2a+b)$$

= .....

= \_\_\_\_\_\_

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(2)	30	$\Delta_{\alpha}$	_ 2)	-4a(	ัว <sub>ส</sub> _	2)
(2	) <i>5a</i> (	<b>4</b> a ·	- 4)	-4a	<b>5</b> a -	- ८)

= .....

= \_\_\_\_\_\_



[3] Simplify 2a(3a-1)+3a(a+2), then find the numerical value of the result when a=1:

$$2a(3a-1)+3a(a+2)$$

= \_\_\_\_\_\_

= \_\_\_\_\_\_

= \_\_\_\_\_\_

= \_\_\_\_\_\_



# Sheet (11) [[ij]iying a binomial by an algebraic expression

#### We have 3 ideas of the examples on this lesson

#### 1<sup>st</sup> idea this is the general idea

#### [1] Find by direct products:

(1) 
$$(x+3)(x+2) =$$

(2) 
$$(x-3)(x-2) =$$

(3) 
$$(x+2)(x-5) =$$

(4) 
$$(y-4)(y+5) =$$

(5) 
$$(x + 2)(x + 4) =$$

(6) 
$$(y-5)(y+2) =$$

(7) 
$$(5m-2)(6m+1)$$
 =

(8) 
$$(4x + 1)(2x + 3) =$$

(9) 
$$(3a + 2b)(2a - 5b) =$$

(10) 
$$(b^2-4)(b^2+2) =$$

(11) 
$$(x-y)(7y-x) =$$



#### 2<sup>nd</sup> idea (special case of 1<sup>st</sup> idea)

#### [2] Find by inspection the expansion of each of the following:

(1) 
$$(x + 2)^2 =$$

(2) 
$$(x + 3)^2 =$$

(3) 
$$(x+1)^2 =$$

(4) 
$$(x-1)^2 =$$

$$(5) (2y + 3)^2 =$$

(6) 
$$(4m-7)^2 =$$

(7) 
$$(3x + y)^2 =$$

$$(8) \quad (x-3y)^2 \quad = \quad \dots$$

(9) 
$$(2x + 3y)^2 =$$

$$(10) (-l-m)^2 =$$

(11) 
$$(-4x-7)^2$$
 =



#### 3<sup>rd</sup> idea special case of 1<sup>st</sup> idea

#### [3] Find by inspection the expansion of each of the following:

(1) 
$$(x + 3)(x - 3) =$$

(2) 
$$(x-4)(x+4) =$$

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(3) (x-2)(x+2) =

 $(4) \quad (4m-7)(4m+7) =$ 

(5) (6x + 2y)(6x - 2y) =

(6)  $(a^2 + a)(a^2 - a) =$ 

(7)  $(3x^2 + 5y^2)(3x^2 - 5y^2) =$ 

(8)  $\left(\frac{1}{2}x + \frac{1}{3}y\right)\left(\frac{1}{2}x - \frac{1}{3}y\right) =$ 



#### [4] Choose the correct answer:

(1) The middle term in the expansion of  $(3x - 1)^2$  is \_\_\_\_\_\_

- (a) 3x
- (b) -6x
- (c) 6x
- (d)  $6x^2$

(2) The middle term in the expansion of  $(2a + 3b)^2$  is

(a) 12ab (b) -12ab (c) 6ab (d) -6ab

(3) If  $(2x + y)^2 = 4x^2 + k x y + y^2$ , then  $k = \dots$ (a) 2 (b) 4 (c) 8 (d) 6

(5) If  $x^2 = 16$ ,  $y^2 = 9$  and xy = 12, then  $(x - y)^2 = \dots$ (a) 49 (b) 165 (c) -1 (d) 1

(6) If  $(x + y)^2 = 26$  and  $x^2 + y^2 = 20$ , then xy = ...(a) 3 (b) 6 (c) 9 (d) 12 Mathematics 1<sup>st</sup> Prep 1<sup>st</sup> term

- If x + y = 7, then the numerical value of  $x^2 + 2xy + y^2 = ...$ **(7)** 
  - (a) 7
- (b) 14
- (c) 49
- (d) 28
- If x y = 3 and x + y = 5, then  $x^2 y^2 = .....$ (8)
  - (a) 2
- (b) -2
- (c) 8
- (d) 15
- (9) If  $x = \frac{4}{3}$ , then  $(x-2)(x+2) = \dots$

- (a)  $\frac{4}{3}$  2 (b)  $\left(\frac{4}{3}\right)^2$  2 (c)  $\left(\frac{4}{3}\right)^2$  4 (d)  $\left(\frac{4}{3}\right)^2$  + 4
- (10) If  $(x-3)(x+3) = x^2 + k$ , then  $k = \dots$ 
  - (a)9
- (b) 6
- (c) -9
- (d) -6
- (11) If  $(x-y)(2x+y) = 2x^2 + k x y y^2$ , then  $|k| = \dots$ 
  - (a) -1
- (b) 1
- (c)3



[5] Multiply, then find the numerical value of the expression when x = 1 and y = -2:

(1) (x-5y)(x+5y)



= .....

(2) (3x + y)(x + 3y)= .....

=

(3) (x + 4)(3x + 2)= .....

=



[6] Reduce	$(x-y)^2$	+ 2 x y	then	find	the	numerical	value	of	the
result when	x = -1	and y =	= <b>-2</b> :						

= \_\_\_\_\_

= .....

= \_\_\_\_\_\_

= .....

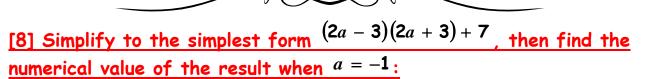
[7] Reduce =  $\frac{(2x-2)^2 + (x-2)(x+2)}{\text{of the result when } x = -1}$ ;

= .....

= .....

= \_\_\_\_\_

= .....



= .....

= \_\_\_\_\_

= .....

= .....

## Sheet (12) Dividing an algebraic expression by a monomial

[1] If the symbols in the following expressions are non-zero numbers, find the quotient in each case:

(1) 
$$5a - 10$$
 by 5 =

(2) 
$$4a^2 + 6a$$
 by  $2a =$ 

(3) 
$$12a^2b + 20a b^2$$
 by  $4a b =$ 

(4) 
$$16a^3b^2 - 24a^2b^2$$
 by  $4a^2b =$ 

(5) 
$$12x + 15y$$
 by  $-3$  =

(6) 
$$24x^3 - 18x^2$$
 by  $-6x^2$  =

(7) 
$$60x^6 - 48x^{10} - 12x^3$$
 by  $-12x^3 =$ 

= .....

(8) 
$$32x^5 - 48x^3 + 72x^7$$
 by  $-8x^3 =$ 

= .....



[2] Find the quotient of each of the following:

(1) 
$$\frac{26x^2 + 14x^4}{2x} =$$

$$(2) \quad \frac{18m^4 + 32m^2}{-2m^2} \quad = \quad \qquad = \quad \qquad = \quad \qquad = \quad \qquad \qquad$$

(3) 
$$\frac{48x^3 - 80x^2}{8x^2} = \dots = \dots$$

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$$(4) \quad \frac{9l^3m^4 - 18l \ m^2}{3l \ m^2} = \dots = \dots$$

### [3] Choose the correct answer:

(1) 
$$(x^2 + x) \div x = \dots, x \neq 0$$
  
(a) zero (b) x (c)  $2x + 1$  (d)  $x + 1$ 

(2) 
$$(15a + 5) \div 5 = \dots$$
  
(a)  $3a$  (b)  $10a$  (c)  $3a + 1$  (d)  $4a$ 

(3) 
$$(4a^3 - 2a) \div (-2a) = \dots, a \neq 0$$
  
(a)  $-2a^2$  (b)  $-2a^2 + 1$  (c)  $2a^2 + 1$  (d) -1

(4) 
$$(15x^4 + 5x^3) \div 5x^3 = \dots$$
  
(a)  $3x^2 + x$  (b)  $5x^2 + 1$  (c)  $3x + 1$  (d)  $4x^4$ 

(5) 
$$(3x^2y - ....) \div 3x \ y = x - 2y$$
  
(a)  $6x$  (b)  $6x \ y^2$  (c)  $6y^2$  (d)  $-6x \ y^2$ 

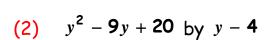
(6) If 
$$(6x^2y^3 + k \ x \ y) \div 6x = x \ y^3 - 12y$$
,  $x \neq 0$ , then  $|k| = \dots$   
(a) -72 (b) -2 (c) 2 (d) 72

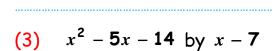


## Sheet (13) Dividing an algebraic expression by another one

### [1] Find the quotient of each of the following:

(1) 
$$x^2 + 5x + 6$$
 by  $x + 2$ 





(4) 
$$2x^2 + 13x + 15$$
 by  $x + 5$ 

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(5) $3x^2 + 2x - 8$ by $3x - 4$
---------------------------------

(6)  $x^2 - 6 - x$  by x + 2

[2] If the area of a rectangle is  $(15x^2 + 11x - 14)$  cm2 and its width is (3x - 2) cm. Calculate its length.

[3] If the area of a rectangle is  $(2x^2 + 7x - 15)$  cm2 and its length is (x + 5) cm. Find its width and calculate its perimeter when x = 3.

# 1-4 Multiplying and dividing rational numbers

### **EXAMPLE:** Find the result of each of the following in its simplest form:

1) 
$$\frac{3}{6} \times \frac{2}{5}$$

2) 
$$-\frac{3}{4} \times \frac{2}{9}$$

3) 
$$\frac{1}{2} \times (-2)$$

4) 
$$-4\frac{2}{7} \times (-3\frac{1}{6})$$

$$5) \quad \frac{3}{2} \times \frac{5}{9}$$

6) 
$$\frac{8}{5} \times \left(-\frac{4}{9}\right)$$

20

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7) -5 × \frac{3}{10}

7) 
$$-5 \times \frac{3}{10}$$

8) 
$$-4\frac{1}{2} \times (-\frac{5}{9})$$

Properties of the set of rational numbers under multiplication

Closure property:

Commutative property:

Associative property:









The existence of multiplicative identity (neutral) element property :



6 Property of distributing multiplication over addition and subtraction :

**EXAMPLE:** Use the distributive property to find each of the following:

9) 
$$\frac{5}{11} \times \frac{6}{7} + \frac{5}{11} \times \frac{1}{7}$$

10) 
$$\frac{9}{17} \times 21 - \frac{9}{17} \times 4$$

11) 
$$\frac{22}{25} \times \frac{6}{11} + \frac{5}{11} \times \frac{22}{25} - \frac{22}{25}$$

12) 
$$\frac{7}{12} \times 5 + \frac{49}{12} - \frac{7}{12} \times 11$$



13) 
$$\frac{5}{7} \times \frac{2}{3} + \frac{5}{7} \times \frac{1}{3}$$

14)  $11 \times \frac{3}{10} - \frac{3}{10}$ 

## **EXAMPLE:** Find the result of each of the following in its simplest form:

15) 
$$-\frac{2}{3} \div \frac{5}{3}$$

16) 
$$\frac{3}{7} \div (-8)$$







24

184 Term

17) 
$$2\frac{1}{5} \div 5\frac{1}{2}$$

18) 
$$0.2 \div \frac{1}{5}$$

19)  $\left(\frac{2}{7} + \frac{3}{7}\right) + \frac{10}{7}$ 

20) 
$$\left(\frac{5}{6} - \frac{3}{4}\right) \div \left(\frac{7}{12} - \frac{5}{9}\right)$$

21)  $\frac{3}{7} \div \frac{9}{14}$ 

22) 
$$\frac{3}{4} \div \left(-\frac{15}{2}\right)$$









23) 
$$2\frac{1}{3} \div \left(-\frac{7}{3}\right)$$

24) 
$$-\frac{5}{6} \div 10$$

### **EXAMPLE:**

If  $x = -\frac{1}{3}$ ,  $y = \frac{3}{4}$  and z = -3, find the numerical value of each of the following:

$$25) \frac{y}{z}$$

$$26) \ \frac{xy}{z}$$

$$27) \frac{x}{y} - \frac{y}{z}$$



### 1-5 applications on the rational numbers

### Example:

1)	Find a rational number lying at one third of t	he way between 2 and 8
2)	Find a rational number in the half way way b	between $\frac{2}{5}$ and $\frac{3}{7}$
		Ty .
	AMPLE: Find a rational number lying at one third o	f the way between 2 and 8
3)	From the side of the smaller number.	
<i>4)</i>	From the side of the greater number.	

Find a rational number lying at one fourth of the way way between  $-\frac{1}{6}$  and  $-\frac{1}{3}$  from the side of the smaller number

Find a rational number lying at one fifth of the way between:  $\frac{2}{5}$  and  $\frac{4}{7}$  from the side of the greater number.

## 2-1 algebraic terms and algebraic expressions

#### **EXAMPLE:**

Write the algebraic term that represents the area of each of the following shapes:

	Thun,	
	To Postano	

### **EXAMPLE:** Complete the following table:

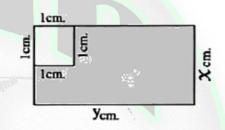
3)

Algebraic term	5 X	3 x y	$-5 a^2$	4 x <sup>2</sup> y	$-2a^2b^2$	15 a <sup>3</sup> b	x	-4	(-3) <sup>2</sup>
Its coefficient									
Its degree									

### **EXAMPLE:** Write the algebraic expression that expresses each of the following:

4) The length of  $\overline{AB}$ 

5) The area of the shaded part



### **EXAMPLE:** Arrange the algebraic expression: $5x + 2x^3 - 4 - x^2$ :

According to the descending order of the indices of x

According to the ascending order of the indices of X

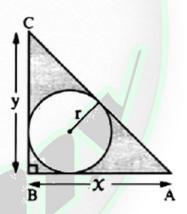
State the degree of the algebraic expression:  $2 a^3 b^2 - 7 a b^3 + 5 a^2 b$ , then arrange it:

- According to the descending order of the indices of a
- 9) According to the ascending order of the indices of b

#### **EXAMPLE:**

10) From the opposite figure:

Write the algebraic expression which represents the area of the coloured part, then state its degree (given that the area of the circle =  $\pi r^2$ )



### Complete the following table:

11)

The algebraic expression	Its terms	The number of terms	Its name	Its degree
$-2a^2b^3$	$-2 a^2 b^3$	1	Monomial	5
$a^3 - 5 a^2 b^2 + 3 b^2$	$a^3 - 5 a^2 b^2 - 3 b^2$		Trinomial	
$\frac{1}{2}a + \frac{1}{4}b - 5$				
$2x^2y + 5xy + 4y$				
$1 - 7 x^2 y$	-//	The state of the s		
$3^2 x^2 + 2^4 x$				

## 2-2 like algebraic 4erms

#### EXAMPLE: Add:

- 1) 5a,3a,a,6a
- 2)  $7ab^2, -2b^2a, -4b^2a, ab^2$

#### **EXAMPLE:** Subtract:

- 3)  $5 \times y$  from  $7 \times y$
- 4)  $2 x^2 y \text{ from } -5 x^2 y$
- $-3 a^2 b^2 \text{ from } 5 a^2 b^2$







6) 
$$-3 x^3 y \text{ from } -2 y x^3$$

### **EXAMPLE:** Put the suitable term in each space:

$$7) \quad 4x + 5x = \boxed{\phantom{a}}$$

8) 
$$2x-4x+x=$$

9) 
$$3x^2 + \boxed{\phantom{0}} = 5x^2$$

10) 
$$7 a^3 - \boxed{\phantom{a}} = 2 a^3$$

11) 
$$2b^4 + = b^4$$

12) 
$$3 y^5 - \boxed{\phantom{0}} = 5 y^5$$







- 13) 4 x is less than 7 x by
- 14) 7 y is more than -2 y by

## **EXAMPLE:** Reduce to the simplest form:

15) 
$$6x+7y+4x-3y$$

16) 
$$6x^2 - 7x - 4x^2 + 5x - 3x + x^2$$

17) 
$$a^2 + 3a - 4 + 4a^2 - 5a + 1$$









18) In the opposite figure:

> Write the algebraic expression that expresses the perimeter of the opposite figure.

	<del>-1-</del>	<b></b> 2X	_
ŧ		*	
*			┦,
-			•

19) In the opposite figure:

> Write the algebraic expression which expresses the sum of the areas of the rectangles which are shown in the opposite figure.

2X	3X <sup>2</sup>
6	9322







2-3 adding and subtracting algebraic expressions

**EXAMPLE:** Add the following expressions:

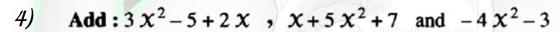
1) 
$$5a-7b+3$$
 and  $2b-1-a$ 

2) 
$$3x^3-4x^2+2x-1$$
,  $5x^2-2x^3+3$  and  $2-3x+x^2$ 



3) Add:  $4x^2 - 3xy + y^2$  and  $3xy - 3x^2 + 2y^2$ 

Then find the numerical value of the result when : x = -2 , y = 1



Then find the numerical value of the result when : x = 2



### **EXAMPLE:** Subtract:

5) 5x-3y+2z from 2y-z+7x

#### **EXAMPLE:**

What is the expression that should be added to  $8 - 3 a^2 + 2 a^3$  to get the result  $5 + 4 a^3 - 7 a$ ?

What is the increase of  $3a^2 - 4b^2 + 2ab$  than the sum of  $2a^2 - 3ab + b^2$  and  $2b^2 + a^2 + ab$ ?

What is the decrease of  $7-5a+a^2$  than  $3a^2-5a-2$ ?

## 2-4 Multiplying and dividing algebraic terms

### **EXAMPLE:** Find the result of the following:

1) 
$$5a^3b \times 3ab$$

2) 
$$\frac{3}{4} a^2 \times \frac{4}{3} a$$

3) 
$$\frac{2}{5} x^2 \times (-15 x^3)$$

4) 
$$2 a \times (-3 ab)$$

$$5) -2 x^2 y \times 3 x y^2$$

6) 
$$\frac{2}{3}$$
 m<sup>2</sup> n ×  $\frac{9}{4}$  n

7) 
$$-4 l m^2 \times \frac{1}{2} l^2 m^2$$

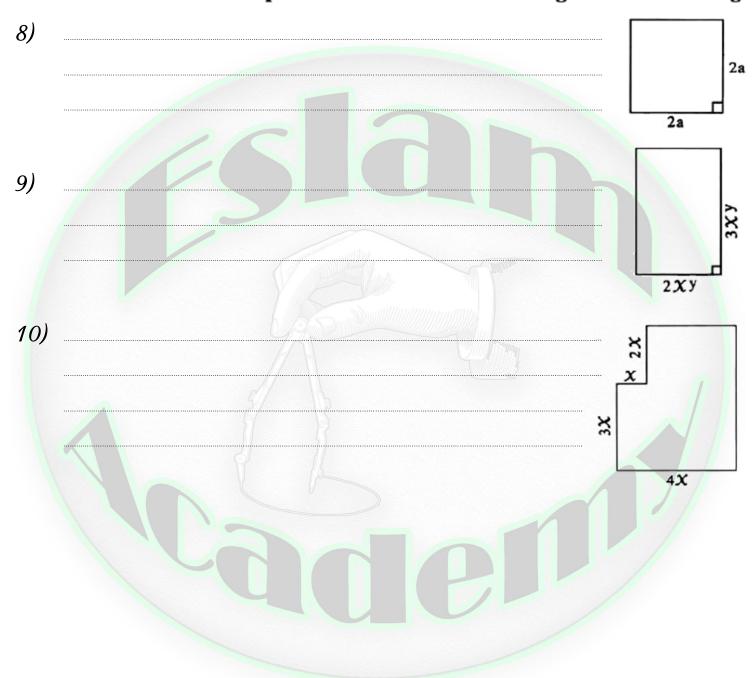




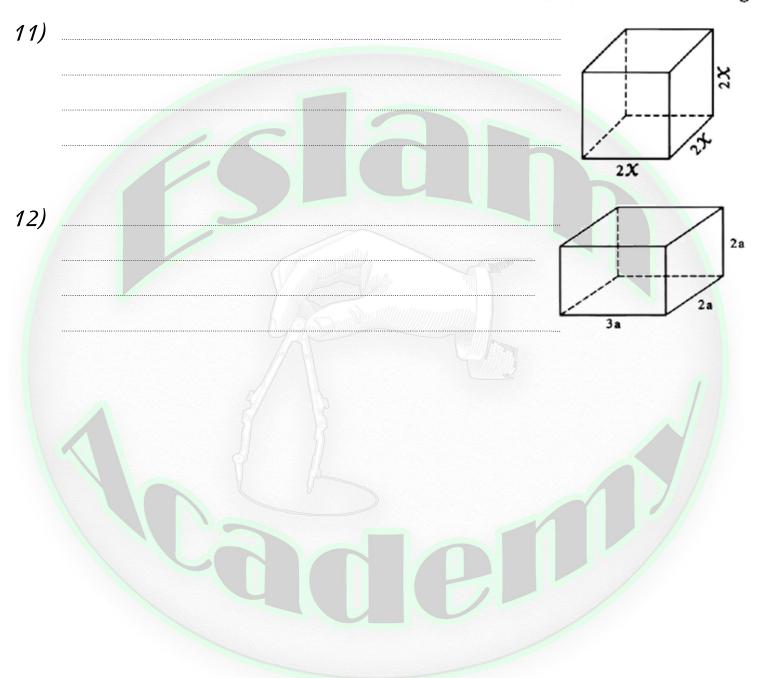




### **EXAMPLE:** Calculate the perimeter and the area of each figure of the following:

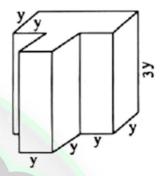


### **EXAMPLE**: Calculate the total surface area and the volume of each solid of the following:



43

13) Find the volume of the opposite solid.



14) A sphere is put inside a cube as shown in the figure to touch all its six faces internally. Find the ratio between the volume of the sphere and that of the cube  $(\pi = \frac{22}{7})$ .



(The volume of the sphere =  $\frac{4}{3} \pi r^3$ )

2-5 Multiplying a monomial by an algebraic expression

### **EXAMPLE:** Find the product of each of the following:

1) 
$$b(-2a+a^2b)$$

2) 
$$-3 a b (5 a - 2 b + 3)$$

3) 
$$(a^2 - ab - 2b^2) \times 4ab$$

4) 
$$3a(2a-4b)$$

$$-2x(3xy-5x)$$

Simplify to the simplest form:  $2 a (a + 4 b) - 3 b (a - 3 b) - (2 a^2 + 8 b^2)$ Then find the numerical value of the result when: a = 1 and b = -2



EXAMPLE: Find the area

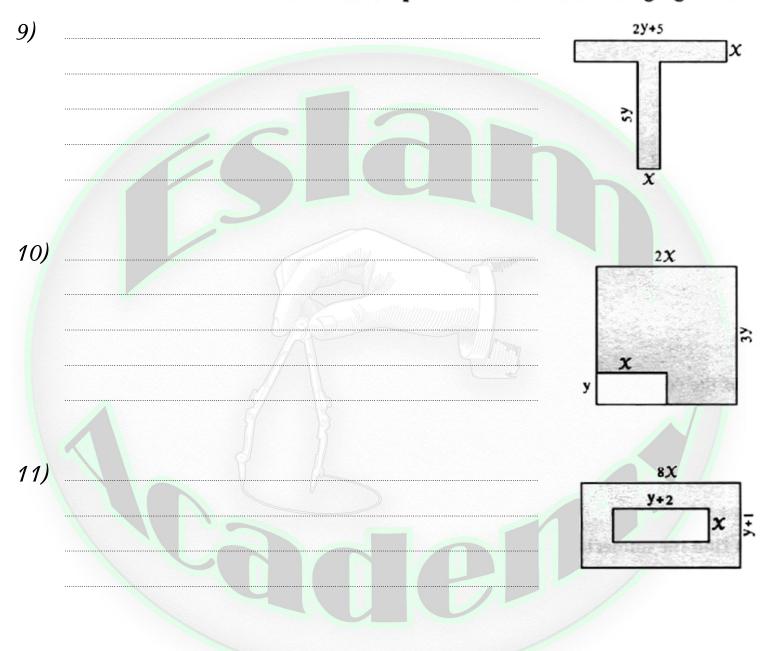
5

x

2x

x

### **EXAMPLE**: Find the area of the coloured part in each of the following figures:



47

## 2-6 Multiplying a binomial by an algebraic expression

#### **EXAMPLE:** Find the product of:

1) 
$$(x+5)(2x-3)$$

2) 
$$(3 x+7)(2 x-3)$$

3) 
$$(2a+3)(5a+1)$$

4) 
$$(3 x+4) (2 x-5)$$

5) 
$$(5a-2b)(7a-3b)$$

6) 
$$(4 \times -3 \text{ y}) (3 \text{ y} + \times)$$

7) 
$$(2a+1)(5a+3)$$

8) 
$$(3 x+4)(2 x-1)$$



#### **EXAMPLE:** Find the expansion of each of the following:

9) 
$$(3a+5)^2$$

10) 
$$(2 \times -3 \text{ y})^2$$

11) 
$$(3 m + 2)^2$$

12) 
$$(2x-3y)^2$$

### **EXAMPLE:** Find the product of each of the following:

13) 
$$(2l-5)(2l+5)$$

14) 
$$(5 X + 3 y) (5 X - 3 y)$$

15) 
$$(a^2 + 2b)(a^2 - 2b)$$

16) 
$$(\frac{1}{3}a - \frac{2}{5}b)(\frac{1}{3}a + \frac{2}{5}b)$$

17) 
$$(2a+3b)(2a-3b)$$

$$(3a-4b)(3a+4b)$$







### **EXAMPLE:** Put each of the following in the simplest form:

19) 
$$(x+4)^2-(x+2)(x+6)$$

20) 
$$(x+5)(x-5)+(x-5)^2$$

### **EXAMPLE:** Find the product of:

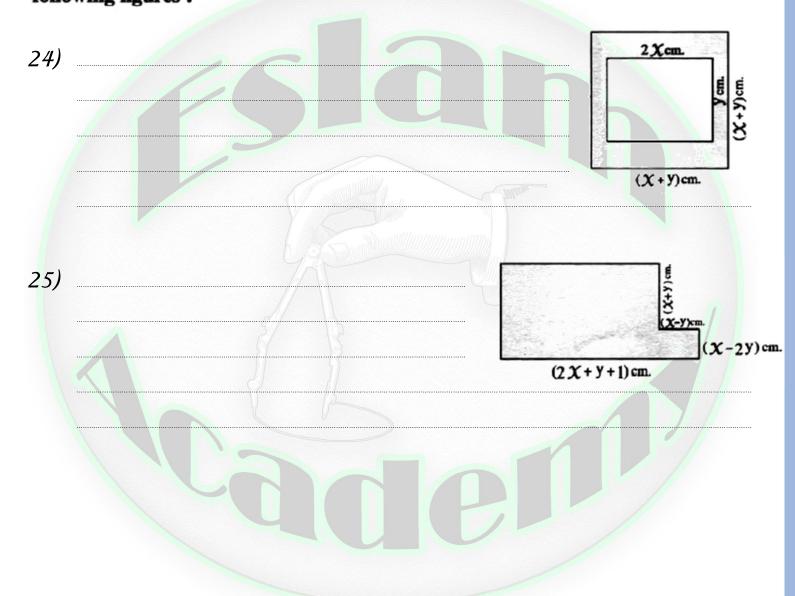
21) 
$$(x-3)(x^2+4x-7)$$

22) 
$$(-3x+x^2+3)(x-2)$$

23)  $3a^3 + a^2 - 4$  by 2a + 3



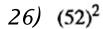
Find the expression which expresses the area of the coloured part in each of the following figures:



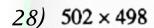
## **EXAMPLE:**

Use the multiplication by inspection to find the value of each of the following easily

the value of:









2-7 Dividing an algebraic expression by a monomial

#### **EXAMPLE:**

Find the quotient in each of the following where the symbols represent integers which aren't equal to zero:

53

1) 
$$\frac{21 x^2 + 14 x}{7 x}$$

2) 
$$\frac{10 a^6 b^4 - 8 a^5 b^3 + 2 a^4 b^2}{2 a^4 b}$$

3) 
$$(16 x^3 y + 8 x^2 y^3 - 12 x^2 y)$$
 by  $(-4 x^2 y)$ 

4) 
$$(12 X^4 + 8 X^2) \div 4 X$$

5) 
$$(14 x^3 - 21 x^2 + 7 x) \div (-7 x)$$

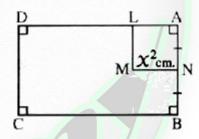
#### **EXAMPLE:**

- 6) Divide:  $\frac{3 \text{ a b}^2 \text{ c} 5 \text{ a}^2 \text{ b c} + 2 \text{ a b c}^2}{\text{a b c}}$  in which abc  $\neq$  zero
  - , then find the absolute value of the result when: a = 1, b = -2 and c = 3

## **EXAMPLE:**

7) In the opposite figure :

ABCD is a rectangle, ANML is a square, N is the midpoint of  $\overline{AB}$  and NM =  $\chi^2$  cm. If the area of the coloured part is  $(\chi^4 + 10 \chi^2)$  cm<sup>2</sup>.



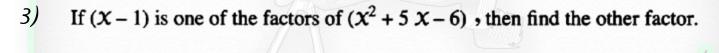
Find the length of LD

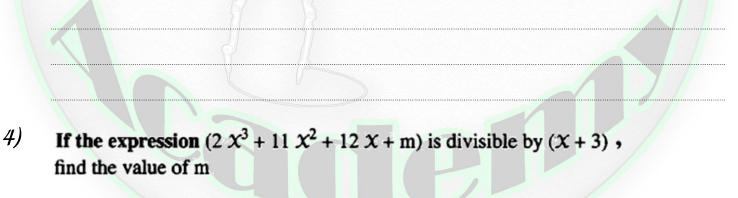
2-8 Dividing an algebraic expression by a another one

# **EXAMPLE:** Find the quotient of dividing:

1) 
$$5 a - 10 a^2 + 6 a^3 + 3 by 3 + 2 a^2 - 4 a$$
 2)  $x^3 + x + 10 by x + 2 where  $x \ne -2$$ 









a If 
$$x = -\frac{1}{3}$$
,  $y = \frac{3}{4}$  and  $z = -3$ , find the numerical value of:  $4xy + z$ 

Solution  $= 4 \times \frac{-1}{3} \times \frac{3}{4} + (-3) = -1 - 3 = -4$ 

b If 
$$x = \frac{3}{4}$$
,  $y = -\frac{5}{2}$ , find in simplest form the value of:

$$(x - y) \div (x + y) = \left(\frac{3}{4} - \left(\frac{-5}{2}\right)\right) \div \left(\frac{3}{4} + \left(\frac{-5}{2}\right)\right)$$

$$= \left(\frac{3}{4} + \frac{10}{4}\right) \div \left(\frac{3}{4} - \frac{10}{4}\right)$$

$$= \frac{13}{4} \div \frac{-7}{4} = \frac{13}{4} \times \frac{-4}{7} = \frac{-13}{7}$$

If 
$$x = \frac{1}{2}$$
,  $y = \frac{-2}{3}$ ,  $z = 2$ , find the value of:  $\frac{y-z}{x}$   
Solution  $y-z = \frac{-2}{3}-2 = \frac{-2}{3}-\frac{6}{3} = \frac{-8}{3} \div \frac{1}{2} = \frac{-8}{3} \times 2 = \frac{-16}{3}$ 

If 
$$X = \frac{2}{3}$$
,  $y = \frac{-3}{4}$ ,  $z = -3$ , find the value of :  $Xy - z$   
Solution  $x = \frac{2}{3} \times (-3) - (-3) = \frac{-1}{2} + 3 = 2\frac{1}{2}$ 

E If 
$$a = \frac{1}{2}$$
,  $b = -\frac{2}{3}$  and  $c = 3$  Find the value of:  $a^2 - 2$  bc  
Solution  $= \left(\frac{1}{2}\right)^2 - 2 \times \left(\frac{-2}{3}\right) \times 3 = \frac{1}{4} + 4 = 4\frac{1}{4}$ 

F If 
$$a = \frac{7}{4}$$
,  $b = \frac{-1}{2}$ , find the value of:  $(a - b) \div (a + b)$ 

Solution  $= (\frac{7}{4} - (\frac{-1}{2})) \div (\frac{7}{4} + (\frac{-1}{2})) = (\frac{7}{4} + \frac{2}{4}) \div (\frac{7}{4} - \frac{2}{4})$ 
 $= \frac{9}{4} \div \frac{5}{4} = \frac{9}{4} \times \frac{4}{5} = \frac{9}{5}$ 

If 
$$X = \frac{3}{2}$$
,  $y = -\frac{1}{4}$  and  $z = -2$ ,

Α

find in the simplest form the numerical value of the following :  $\chi - (z \div y)$ 

Solution 
$$= \frac{3}{2} - \left[ -2 \div \left( -\frac{1}{4} \right) \right]$$
$$= \frac{3}{2} - \left[ -2 \times \left( -4 \right) \right] = \frac{3}{2} - 8 = -\frac{13}{2}$$

If the two rational numbers  $\frac{3 \, x}{4}$  and  $\frac{2}{3}$  are equal, find the value of x

B Solution 
$$\frac{3x}{4} = \frac{2}{3}$$
  $x = \frac{4 \times 2}{3 \times 3} = \frac{8}{9}$ 

If  $a = \frac{3}{4}$ ,  $b = -\frac{5}{2}$ , without using calculator find the value of: 4a - 6b

C Solution The numerical value = 
$$4 \times \frac{3}{4} - 6 \times \frac{-5}{2} = 3 + 15 = 18$$

Find in the simplest form the value of each of the following:

(1) 
$$-15\frac{1}{4} + 12\frac{1}{2}$$
  
Solution  $-15\frac{1}{4} = -\frac{61}{4}$ ,  $12\frac{1}{2} = \frac{25}{2}$   
 $-15\frac{1}{4} + 12\frac{1}{2} = \frac{-61}{4} + \frac{50}{4} = -\frac{11}{4} = -2\frac{3}{4}$   
Solution  $0.18 = \frac{2}{11}$ ,  $25\% = \frac{1}{4}$   
 $\frac{2}{11} - \frac{1}{4} = \frac{8}{44} - \frac{11}{44} = -\frac{3}{44}$ 

If  $a = \frac{7}{4}$ ,  $b = \frac{1}{2}$ , find the numerical value of the expression:  $\frac{a-b}{a+b}$ 

$$a-b = \frac{7}{4} - \frac{1}{2} = \frac{7}{4} - \frac{2}{4} = \frac{5}{4}$$

$$\frac{a-b}{a+b} = \frac{5}{4} \times \frac{4}{9} = \frac{5}{9}$$

學也	************************			
av.	Find the rational number that lies halfway between: $\frac{1}{2}$ and $\frac{4}{5}$			
А	Solution The number = $\left(\frac{1}{2} + \frac{4}{5}\right) \div 2 = \frac{13}{20}$			
	Find a rational number lying at :			
	(1) One fourth of the way between $\frac{5}{7}$ , $-\frac{3}{7}$ from the side of the smaller number.			
	Solution The distance between the two numbers			
В	$=\left \frac{5}{7}-\left(-\frac{3}{7}\right)\right =\left \frac{5}{7}+\frac{3}{7}\right =\frac{8}{7}$			
	Then the number $= -\frac{3}{7} + \frac{1}{4} \times \frac{8}{7} = -\frac{3}{7} + \frac{2}{7} = -\frac{1}{7}$			
	One fifth of the way between $-\frac{1}{2}$ , $-\frac{2}{5}$ from the side of the greater number.			
С	Solution			
	The distance between the two numbers  Then the number			
	$= \left  -\frac{1}{2} - \left( -\frac{2}{5} \right) \right  = \left  -\frac{1}{2} + \frac{2}{5} \right  = \left  -\frac{5}{10} + \frac{4}{10} \right  = \frac{1}{10}$ $= -\frac{4}{10} - \frac{1}{5} \times \frac{1}{10} = -\frac{4}{10} - \frac{1}{50} = \frac{-20 - 1}{50} = -\frac{21}{50}$			
	One tenth of the way between $\frac{5}{6}$ , $\frac{2}{3}$ from the side of the smaller number.			
D	Solution			
	The distance between the two numbers 4 1 1 4 1			
	Then the number = $\frac{15}{6} + \frac{2}{10} \times \frac{2}{6} = \frac{1}{6} + \frac{1}{60}$			
	$= \frac{40+1}{60} = \frac{41}{60}$			
	Find the number one fourth of the way between $-\frac{1}{4}$ and $-\frac{7}{8}$ from the side of the smaller number.			
E				
F	Find the number that lies one third of the way between $\frac{1}{4}$ and $\frac{7}{8}$ from the side of the smaller one.			
G	Find the rational number that lies half way between : $\frac{1}{2}$ , $\frac{1}{5}$			
Н	Find the rational number that lies halfway between : $\frac{1}{2}$ and $\frac{4}{5}$			
<b>⊕</b>	Mahmoud Ezz Al deen			

Find three rational numbers lying between

A 
$$\frac{1}{4}$$
 and  $\frac{1}{5}$ 

First 
$$\frac{1 \times 5}{4 \times 5} = \frac{5 \times 10}{20 \times 10} = \frac{50}{100}$$

Second 
$$\frac{1 \times 4}{1 \times 5} = \frac{4 \times 10}{20 \times 10} = \frac{40}{100}$$

three rational numbers = 
$$\frac{41}{100} / \frac{42}{100} / \frac{43}{100}$$

Find three rational numbers between:  $\frac{1}{2}$  and  $\frac{1}{3}$ 

First 
$$\frac{1 \times 3}{2 \times 3} = \frac{3 \times 10}{6 \times 10} = \frac{30}{60}$$

Second 
$$\frac{1 \times 2}{3 \times 2} = \frac{2 \times 10}{6 \times 10} = \frac{20}{60}$$

three rational numbers = 
$$\frac{21}{60}$$
 /  $\frac{22}{60}$  /  $\frac{23}{60}$ 

Write three rational numbers between:  $\frac{4}{9}$  and  $\frac{5}{6}$ 

First 
$$\frac{4 \times 6}{9 \times 6} = \frac{24}{54}$$

Second 
$$\frac{5 \times 9}{6 \times 9} = \frac{45}{54}$$

three rational numbers 
$$\frac{24}{54}$$
 /  $\frac{25}{54}$  /  $\frac{26}{54}$ 

**\*** 

What is the increase of :

$$3 x^2 - 5 x + 2$$
than  $7 x^2 - x - 3$ ?

Solution 
$$3x^2 - 5x + 2$$
Increase  $3x^2 - 5x + 2$ 
 $7x^2 - x - 3$ 
Increase  $7x^2 - x - 3$ 
Increase  $7x^2 - 4x + 5$ 

What is the increase of:

$$4x^2-6x+5$$
 than  $7x^2-x-9$ 

Solution

Add the two expressions

$$7 X - 3 y - 1$$
 and  $2 X + 5 y + 3$ 

Solution 
$$7x-3y-1$$
  
 $2x+5y+3$   
 $9x+2y+2$ 

في حاله الجمع والطرح متجيش جمب الاسس و الرموز ي حمار تنزل ذي ما هي ما عدا الصفر

**C** Add: 2 X - 6 z + y, 3 y + 2 z - 5 X

**Add:**  $3 x^2 - 5 x + 1$  and  $x^2 + x + 3$ 

**Add:**  $5 x^2 + y^2 - 3 x y$  and  $x^2 - 2 x y + 3 y^2$ 

Example 2 Add the following expressions:

$$3x^3-4x^2+2x-1$$
,  $5x^2-2x^3+3$  and  $2-3x+x^2$ 

The first expression :  $3 x^3 - 4 x^2 + 2 x - 1$ 

The second expression :  $-2 x^3 + 5 x^2 + 3$ 

The third expression :  $+ x^2 - 3x + 2$ 

The sum =  $x^3 + 2x^2 - x + 4$ 

Α

Example 4 Subtract: 5x-3y+2z from 2y-z+7x

Solution

$$: 2y -z + 7x$$

$$= \frac{0.00}{5 \text{ y} + 2 \text{ z} + 5 \text{ x}}{0.000}$$

في حالة subtract from ال بعد from يكتب في السطر الاول واغير اشاره الاول

В

**Subtract**:  $y^3 + 5y^2 - 5y$  from  $2y - y^3 + 5y^2$ 

Subtract:  $5x^2 + y^2 - 3xy + 1$  from  $6x^2 - 2xy + 3y^2$ 

Subtract:  $-2x^2 - 5xy + 4y^2$  from  $3x^2 + 2xy + 4y^2$ 

**\$** 

**A** • 2 a × 5 b = 
$$(2 \times 5) \times (a \times b) = 10$$
 a b

**B** • 
$$(5 X^2) \times (3 X) = (5 \times 3) \times (X^2 \times X) = 15 X^3$$

C  $2 \hat{x} (3 x + 5 y) = (2 x \times 3 x) + (2 x \times 5 y)$ =  $6 x^2 + 10 x y$ 

$$\begin{array}{c} 3x + 5y \\ \times 2x \end{array}$$

The product =  $6 x^2 + 10 x y$ 

Example 2 Find by inspection the product of each of the following:

(2 a + 3) (5 a + 1)

Example 3 Find the expansion of each of the following:

1 
$$(3 a + 5)^2$$

2 
$$(2 X - 3 y)^2$$

Solution

1 
$$(3 a + 5)^2 = (3 a)^2 + (2 \times 3 a \times 5) + (5)^2$$
  
=  $9 a^2 + 30 a + 25$ 

2 
$$(2 X - 3 y)^2 = (2 X)^2 - (2 \times 2 X \times 3 y) + (3 y)^2$$
  
=  $4 X^2 - 12 X y + 9 y^2$ 

Example Find the product of each of the following:

1 
$$(2l-5)(2l+5)$$

2 
$$(5 X + 3 y) (5 X - 3 y)$$

3 
$$(a^2+2b)(a^2-2b)$$

1 
$$(2 l - 5) (2 l + 5)$$
  
2  $(5 x + 3 y) (5 x - 3 y)$   
3  $(a^2 + 2 b) (a^2 - 2 b)$   
2  $(5 x + 3 y) (5 x - 3 y)$   
4  $(\frac{1}{3} a - \frac{2}{5} b) (\frac{1}{3} a + \frac{2}{5} b)$ 

Solution

1 
$$(2l-5)(2l+5) = (2l)^2 - (5)^2 = 4l^2 - 25$$

2 
$$(5 X + 3 y) (5 X - 3 y) = (5 X)^2 - (3 y)^2 = 25 X^2 - 9 y^2$$

3 
$$(a^2 + 2b) (a^2 - 2b) = (a^2)^2 - (2b)^2 = a^4 - 4b^2$$

4 
$$\left(\frac{1}{3} a - \frac{2}{5} b\right) \left(\frac{1}{3} a + \frac{2}{5} b\right) = \left(\frac{1}{3} a\right)^2 - \left(\frac{2}{5} b\right)^2 = \frac{1}{9} a^2 - \frac{4}{25} b^2$$

**\*** 

**Simplify**: 
$$(y - 5) (y + 2)$$

Solution 
$$(y \otimes y) (2 \otimes y - 5 \otimes y) (-5 \otimes 2)$$
  $\equiv y^2 - 3y - 10$   
 $y^2 \quad 2y - 5y = -3y \quad -10$ 

Simplify to the simplest form :  $(2 \times -3) (2 \times +3) + 7$ 

Solution 
$$(2x \otimes 2x)(3 \otimes -3) = 4 x^2 - 9 + 7 = 4 x^2 - 2$$

**Simplify**: 
$$(X + 2)^2 + (X - 2)(X + 2)$$

Solution 
$$(x \otimes x) + (2 \otimes x \otimes 2) (2 \otimes 2) = x^2 + 4x + 4$$
  
 $(x \otimes x)$   $(2 \otimes -2) = x^2$ 

Find: 
$$(2 X - y) (2 X + y)$$
 Solution  $4 X^2 - y^2$ 

Simplify:  $(X+3)^2-9$ , then find the numerical value when X=3

Solution The expression = 
$$x^2 + 6x + 9 - 9 = x^2 + 6x$$

(3 b - 4) (3 b + 4) + 5, then find the numerical value of the result when b = -2

Solution The expression = 
$$9b^2 - 16 + 5 = 9b^2 - 11$$
  
The numerical value =  $9 \times (-2)^2 - 11 = 9 \times 4 - 11$ 

Simplify to the simplest form: 
$$(x+3)^2 - (x+3)(x-3)$$

6 Mahmoud Ezz Al deen 6 6 6 24 6 6 6 6 11155343556 6 6 6 6

= 36 - 11 = 25

$$= x^{2} + 6x + 9 - (x^{2} - 9) = x^{2} + 6x + 9 - x^{2} + 9 = 6x + 18$$

Simplify: (2 a - 3) (2 a + 3) + 7, then find the value of the result when a = 1

Solution

The expression = 
$$4 a^2 - 9 + 7 = 4 a^2 - 2$$

The numerical value = 
$$4 \times 1^2 - 2 = 4 - 2 = 2$$

Simplify: 2 a (a-4 b) + 4 b (2 a-3 b), then find the value of the result at: a=2, b=-1

Solution

The expression = 
$$2 a^2 - 8 a b + 8 a b - 12 b^2$$
  
=  $2 a^2 - 12 b^2$ 

The numerical value = 
$$2 \times 2^2 - 12 \times (-1)^2$$
  
=  $2 \times 4 - 12 \times 1 = 8 - 12 = -4$ 

Simplify to the simplest form :  $(X - 5)^2 + 10 X$ 

Solution = 
$$x^2 - 10x + 25 + 10x = x^2 + 25$$

Find the product of:  $(3 \times -4 \text{ y}) (2 \times +5 \text{ y})$ 

$$6 x^2 + 7 x y - 20 y^2$$

Simplify to the simplest form: (X-3)(X+3)+9, then

calculate the numerical value of the result when x = 5

Simplify: 3 a (a - b) + 4 a (2 a + b) in the simplest form.

**Solution** ) 
$$3a^2 - 3ab + 8a^2 + 4ab = 11a^2 + ab$$

Simplify: (X-3)(X+3)-9(X-1)

(a) 
$$x^2 - 9 - 9x + 9 = x^2 - 9x$$

Use the distributive property to find:  $\frac{17}{12} \times \frac{23}{45} + \frac{7}{12} \times \frac{23}{45} - 2 \times \frac{23}{45}$ 

**Solution** 
$$\left(\frac{17}{12} + \frac{7}{12} - 2\right) \times \frac{23}{45} = \left(\frac{24}{12} - 2\right) \times \frac{23}{45} = \text{zero}$$

**Simplify**:  $(2 X + 5)^2 - 4 X^2 - 10 X$ 

**Solution** 
$$4x^2 + 20x + 25 - 4x^2 - 10x = 10x + 25$$

Simplify to the simplest form: (X-3)(X+3)+9, then

calculate the numerical value of the result when x = 5

Simplify to the simplest form:  $(2 \times -3) (2 \times +3) + 7$ , then calculate the numerical

value of the result when : X = -1

Simplify to the simplest form :  $(X + 2)^2 - (X + 2)(X - 2)$ 

Simplify the following expression to its simplest form:

$$(X-2)^2 - (X+3)(X-3) + 5(2X+1)$$

Find by inspection method the product of: (X-2)(X+2)

Find the product of:  $(2 \times -3 \text{ y}) (3 \times +7 \text{ y})$ 

Find the product of:  $(3 \times -4 \text{ y}) (2 \times +5 \text{ y})$ 

Simplify to the simplest form:  $(X+3)^2 - (X+3)(X-3)$ 

Simplify to the simplest form :

 $3(1-2a)-(a^2-5a+3)+2a(a+3)$ , then find the numerical value when a=2

Simplify to the simplest form :  $(X - 5)^2 + 10 X$ 

Simplify: (y-5)(y+2)

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# Example Find the quotient of dividing :

$$5 a - 10 a^2 + 6 a^3 + 3$$
 by  $3 + 2 a^2 - 4 a$  where the divisor  $\neq 0$ 

Solution

$$\begin{array}{c|c}
2 a^{2} - 4 a + 3 \\
\hline
3 a + 1
\end{array}$$

$$\begin{array}{c}
6 a^{3} - 10 a^{2} + 5 a + 3 \\
 & - \\
6 a^{3} - 12 a^{2} + 9 a
\end{array}$$

$$\begin{array}{c}
2 a^{2} - 4 a + 3 \\
 & - \\
2 a^{2} - 4 a + 3
\end{array}$$

i.e. The quotient = 3 a + 1

#### Notice that : J

Each of the dividend and the divisor is in a descending order according to the power of "a".

Example 2 Find the quotient of dividing:

$$x^3 + x + 10$$
 by  $x + 2$  where  $x \ne -2$ 

Solution

Notice that : J

There is no term with  $X^2$  in dividend  $\cdot$  so we leave its place empty.

**Example 3** If (x-1) is one of the factors of  $(x^2+5x-6)$ , then find the other factor.

Solution The other

The other factor is the quotient of dividing

$$x^2 + 5x - 6$$
 by  $(x - 1)$ 

i.e. The quotient =  $x^2 - 2x + 5$ 

**i.e.** The other factor is (x + 6)

$$\frac{\begin{array}{c}
x-1 \\
x+6
\end{array}}{\begin{array}{c}
x^2+5x-6 \\
-x^2-x
\end{array}}$$

$$\frac{\begin{array}{c}
6x-6 \\
-6x-6
\end{array}}{\begin{array}{c}
00&00
\end{array}}$$

\$

**Divide**: 
$$(x^2 + 5x + 6)$$
 **by**  $(x + 2)$ 

$$\begin{array}{c|c}
x+3 \\
 \hline
x+2 \\
 \ominus x^2 + 5x + 6 \\
 \ominus x^2 + 2x \\
 \hline
3x+6 \\
 \ominus G \\
 \hline
3x+6 \\
 \hline
0 0
\end{array}$$

The quotient = x + 3

$$x^2 + 5x + 6$$
 by  $x + 3$ 

$$\begin{array}{c|c}
x+2 \\
 \hline
x+3 \\
 \ominus \\
x^2+5x+6 \\
 \ominus \\
x^2+3x \\
 \hline
2x+6 \\
 \ominus \\
2x+6 \\
 \hline
0 & 0
\end{array}$$

The quotient = x + 2

**Divide**:  $6 x^2 + 13 x y + 6 y^2$  by 2 x + 3 y

$$\begin{array}{c|c}
2x+3y \\
\hline
3x+2y \\
\hline
6x^2+13xy+6y^2 \\
6x^2+9xy \\
\hline
4xy+6y^2 \\
9xy \\
6x^2+9xy
\end{array}$$

The quotient =  $3 \times + 2 \text{ y}$ 

 $16 x^2 - 24 x y + 9 y^2$  by 4 x - 3 y

The quotient =  $4 \times -3 \text{ y}$ 

**Divide**:  $(x^2 - 5x + 6)$  **by** (x - 3) (where  $x \ne 3$ )

Find the quotient of:  $x^2 - 2x - 8$  by (x - 4) (where  $x \ne 4$ )

Find the quotient of:  $X^3 + 3X^2 - X - 3$  by  $X^2 - 1$  (where  $X^2 - 1 \neq 0$ )

Divide:  $6 X^2 + 13 X y + 6 y^2$  by 2 X + 3 y (where  $2 X + 3 y \neq 0$ )

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**Divide**:  $6 x^2 y - 9 x y^2 + 24 x y$  by x y

Solution 
$$\frac{6x^2y - 9xy^2 + 24xy}{xy} = 6x + 9y 24$$

**Divide**:  $30 x^3 - 25 x^2 + 15 x$  by 5 x (where  $x \ne 0$ )

Solution 
$$\frac{30 x^3 - 25 x^2 + 15 x}{5 x} = 6 x^2 - 5 x + 3$$

Find the quotient of:  $30 a^2 b^3 - 25 a^3 b^2 + 35 ab$  by 5 a b

Solution 
$$\frac{30 a^2 b^3 - 25 a^3 b^2 + 35 a b}{5 a b} = 6 a b^2 - 5 a^2 b + 7$$

**Divide**:  $x^3 y^3 - 4 x^2 y^2 + 6 x y^2$  **by** x y (where:  $x y \ne 0$ )

Solution 
$$\frac{x^3 y^3}{x y} - \frac{4 x^2 y^2}{x y} + \frac{6 x y^2}{x y} = x^2 y^2 - 4 x y + 6 y$$

The necessary condition to make  $\frac{5}{x-3}$  a rational number is ......

(a) 
$$X = -3$$

(b) 
$$x = 3$$

(c) 
$$X \neq 3$$

(d) 
$$X = 5$$

$$(a^2 + a) \div a = \dots$$
 (where  $a \ne 0$ )

(c) 
$$2a + 1$$

(c) 
$$2a + 1$$
 (d)  $a + 1$ 

$$\frac{3 \times 7}{7} - \frac{\times}{7} = \dots$$

(a) 
$$\frac{2}{7}$$

(b) 
$$\frac{x}{7}$$

(a) 
$$\frac{2}{7}$$
 (b)  $\frac{x}{7}$  (c)  $\frac{2x}{7}$ 

**Divide**: 
$$2 X^3 + 11 X^2 + 12 X - 9$$
 **by**  $X + 3$ 

$$2x^2 + 5x - 3$$

Solution

$$\begin{array}{c|c}
x+3 \\
\hline
2x^2+5x-3 \\
 & 2x^3+11x^2+12x-9 \\
 & 2x^3+6x^2 \\
\hline
 & 5x^2+12x-9 \\
 & 9 \\
 & 5x^2+15x \\
\hline
 & -3x-9 \\
 & 9 \\
 & -3x-9 \\
\hline
 & 0 & 0
\end{array}$$

The quotient =  $2 x^2 + 5 x - 3$ 

**Divide**:  $10 X^4 - 5 X^3$  **by**  $5 X^2$  (if  $X \neq 0$ )

**Divide**:  $x^3 y^3 - 4 x^2 y^2 + 6 x y^2$  **by** x y (where:  $x y \ne 0$ )

(1) Add:  $3 \times -2 y + 5$  and  $2 \times + y - 3$ 

(a) Divide:  $6 X^3 y^3 + 4 X y^2$  by 2 X y (where  $X y \neq 0$ )

**Divide**:  $6 x^3 y^2 + 9 x^2 y^3$  **by**  $3 x^2 y^2$  (where  $x \ne 0, y \ne 0$ )

**Divide**:  $30 X^3 - 25 X^2 + 15 X$  **by** 5 X (where  $X \neq 0$ )

Find the quotient of:  $(X^2 + 5X + 6)$  by (X + 2) (where  $X \neq -2$ )

Find the quotient of:  $(X^3 - 6X^2 + 11X - 6)$  by (X - 3) (where  $X \neq 3$ )

**Divide**:  $2 x^3 + 11 x^2 + 12 x - 9$  **by** x + 3 (where  $x \ne -3$ )

Find the quotient of:  $13 \times + 15 + 2 \times^2$  by  $\times + 5$  (where  $\times \neq -5$ )

Find the value of k which makes the expression:  $2 \times^3 - \times^2 - 5 \times + k$  divided by  $2 \times -3$ 

Find the quotient:  $6 X^2 - X y - 15 y^2$  by 2 X + 3 y (where  $2 X + 3 y \neq 0$ )

**Factorize by using (H.C.F)**: 3 a (a - 2 b) + 7 b (a - 2 b)

Solution (a-2b)(3a+7b)

Factorize by taking the H.C.F:  $15 \times y^3 + 20 \times^2 y - 25 \times y$ 

Solution 5 x y (3  $y^2 + 4x - 5$ )

Factorize the expression by identifying the H.C.F:  $12 y^3 + 18 y^2$ 

Solution  $6 y^2 (2 y + 3)$ 

If X + 4 = 4, then find: X(X + 4) + 4(4 + X)

Where X + 4 = 4, then X = 0then the value  $= 0 \times (0 + 4) + 4 \times (4 + 0)$  $= 0 \times 4 + 4 \times 4 = 0 + 16 = 16$   $(X + 4)(X + 4) = 4 \times 4 := 16$ 

Factorize by identifying the H.C.F:  $3 x^2 + 15 x y$ 

Solution 3x(x+5y)

Subtract: -5 x from 3 x Solution 3 x + 5 x = 8 x

Factorize by identifying the H.C.F.:  $12 \times^3 + 8 \times^2 - 4 \times$ 

Solution  $4 \times (3 \times^2 + 2 \times -1)$ 

By using the highest common factor, find the result of:  $(17)^2 - 8 \times 17 + 17$ 

Solution )  $17(17-8+1)=17\times 10=170$ 

 $\frac{6}{37} \times 7 + \frac{6}{37} \times 5 + \frac{6}{37} \times (-11)$  Solution  $\frac{6}{37} \left(7 + 5 + (-11)\right) = \frac{6}{37} \times 1 = \frac{6}{37}$ 

Factorize by identifying the H.C.F: 3 a (a-2 b) - 6 b (a-2 b)

, then find the numerical value of the result when  $a-2b=\left|\frac{-1}{3}\right|$ 

Solution

The expression =  $3(a-2b)(a-2b) = 3(a-2b)^2$ 

The numerical value =  $3 \times (\frac{1}{3})^2 = 3 \times \frac{1}{9} = \frac{1}{3}$ 

Factorize by identifying the H.C.F:  $6 x^4 y^3 - 12 x^3 y^4 + 2 x^3 y^3$ 

Solution

) 
$$2 x^3 y^3 (3 x - 6 y + 1)$$

Factorize by taking out the H.C.F:  $27 \times^3 - 18 \times^2 + 6 \times$ 

Solution ) 
$$3 \times (9 \times^2 - 6 \times + 2)$$

Simplify:  $3(1-2x)-(x^2-5x+3)+2x(x+3)$ 

• then find the numerical value of the result when x = -1

Solution

$$3-6x-x^2+5x-3+2x^2+6x=x^2+5x$$
  
at  $x=-1$ 

The numerical value =  $(-1)^2 + 5(-1) = 1 - 5 = -4$ 

Factorize by identifying the H.C.F: a(a-2b)-2b(a-2b)

Solution 
$$(a-2b)(a-2b) = (a-2b)^2$$

Factorize by identifying the H.C.F: a(a-2b)-2b(a-2b)

, then find the numerical value of the result when  $(a-2b) = \frac{1}{3}$ 

Solution 
$$(a-2b)(a-2b) = (a-2b)^2$$

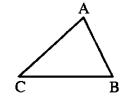
at 
$$(a-2b) = \frac{1}{3}$$
 The numerical value  $= \left(\frac{1}{3}\right)^2 = \frac{1}{9}$ 

# Sheet (5) Congruent triangles

We know that any triangle has three sides and three angles which are known as the six elements of the triangle.

#### For example:

 $\triangle$  ABC has three sides which are :  $\overline{AB}$ ,  $\overline{BC}$  and  $\overline{AC}$  and it has three angles which are :  $\angle A$ ,  $\angle B$  and  $\angle C$ 



#### Therefore:

The two triangles are congruent if each element of the 6 elements of one of them is congruent to the corresponding element in the other triangle and vice versa.

• To test whether two triangles are congruent or not, you don't need to test all the three sides and the three angles.

# The cases of congruence of two triangles

Case (1)

Case (2)

Case (3)

Case (4)

Two sides and the included angle

Two angles and one side

Three sides

Hypotenuse and one side in the right-angled triangle

S. A. S.

A. S. A.

S. S. S.

R. H. S.

Two triangles are congruent if two sides and the included angle of one triangle are congruent to the corresponding parts of the other triangle

Two triangles are congruent if two angles and the side drawn between their vertices of one triangle are congruent to the corresponding parts of the other triangle

Two triangles are congruent if <u>each</u>
<u>side</u> of one triangle is congruent to the corresponding side of the other triangle

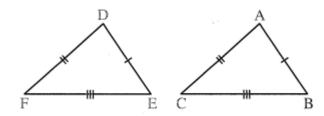
Two right-angled
triangles are
congruent if the
hypotenuse and a
side of one triangle
are congruent to the
corresponding parts
of the other triangle



#### Remark

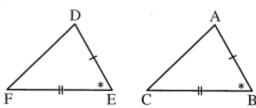
If each angle of one triangle is congruent to the corresponding angle of the other triangle, it is not necessary for the two triangles to be congruent.





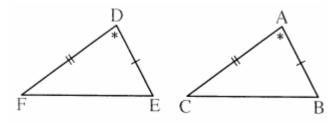
Prove that  $\triangle$  A B  $C \equiv \triangle$  D E F



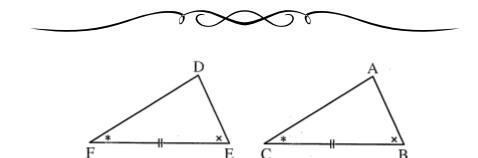


Prove that  $\triangle$  A B  $C \equiv \triangle$  D E F

# Mathematics 1<sup>st</sup> Prep 1<sup>st</sup> term

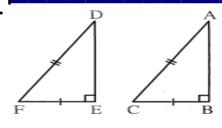


Prove that  $\Delta$  A B  $C \equiv \Delta$  D E F



Prove that  $\triangle ABC \equiv \triangle DEF$ 

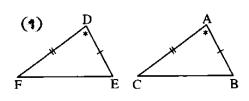
Mathematics 1<sup>st</sup> Prep 1<sup>st</sup> term

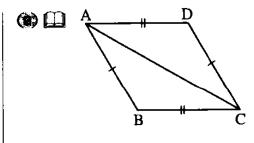


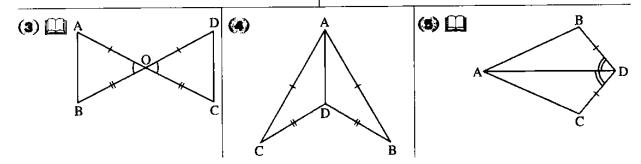
Prove that  $\triangle ABC \equiv \triangle DEF$ 



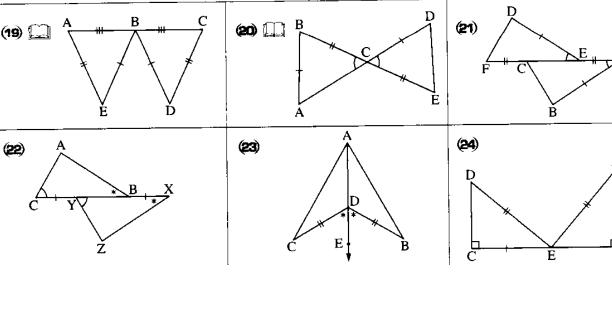
[1] In each of the following figures, show if the two triangles are congruent or not. If they are congruent, name the case of congruence. If they aren't congruent, give reason. (given that the similar signs denoted the congruency of the elements marked by these signs).





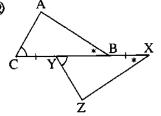


# Mathematics 1st Prep 1st term (8) 🛄 **(7**) (6) (11) 🛄 (10) D (9) (1) E (14) (12) III F D D (16) (15) 🛄 D (18) (17) (20) III B **(21**) (19) 🛄

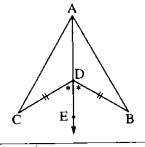


#### Mathematics 1st Prep 1st term

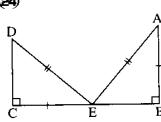
(22)



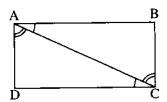
(23)



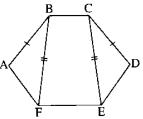
(24)



(25) 🛄



(58)





#### [2] Answer the following:

(1) In the opposite figure:

These triangles are congruent

, then  $X = \cdots \circ$ 





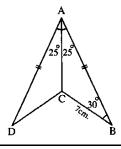
(2) In the opposite figure:

If: AB = AD, BC = 7 cm.,  $m (\angle BAC) = m (\angle DAC) = 25^{\circ}$ 

and m ( $\angle$  B) = 30°

Complete the following:

- $(1) \Delta ACB \equiv \Delta \cdots$
- (2) m (∠ D) = ······°
- (3) CD = ..... cm.
- (4) m (∠ ACD) = ······°

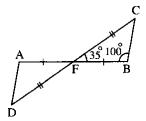


(3) In the opposite figure:

If:  $\overrightarrow{CD} \cap \overrightarrow{BA} = \{F\}$ , FA = FB, CF = FD,

 $m (\angle CFB) = 35^{\circ} \text{ and } m (\angle B) = 100^{\circ}$ ,

then m ( $\angle$  D) = ······°



(4) In the opposite figure:

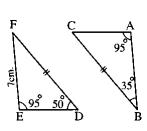
If: BC = FD,  $m (\angle A) = m (\angle E) = 95^{\circ}$ ,

 $m (\angle B) = 35^{\circ}$ ,  $m (\angle D) = 50^{\circ}$  and FE = 7 cm.

Complete the following:

- (1) m ( $\angle$  C) = ······°
- (**2**) m (∠ F) = ······°
- (3)  $\triangle$  ABC  $\equiv$  .....

- (4) AC ≡ .....
- (5)  $AB = \cdots cm$ .

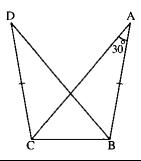


# (5) In the opposite figure:

If : AB = DC  $\cdot$  AC = DB and m ( $\angle$  A) = 30°

#### **Complete the following:**

- (1)  $\triangle$  ABC  $\equiv$   $\triangle$  ......
- (**2**) m (∠ D) = ······°
- (3) m ( $\angle$  DBC) = m ( $\angle$  ······)



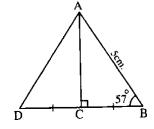
#### (6) In the opposite figure:

C is the midpoint of  $\overline{BD}$  ,  $\overline{AC} \perp \overline{BD}\,$  ,

AB = 5 cm. and m ( $\angle$  B) = 57°

Find: (1) The length of  $\overline{AD}$ 

**(2)** m (∠ DAC)

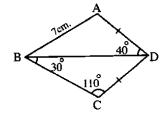


#### (7) In the opposite figure:

AD = DC,  $m (\angle ADB) = 40^{\circ}$ ,  $m (\angle DBC) = 30^{\circ}$ ,

 $m (\angle BCD) = 110^{\circ} \text{ and } AB = 7 \text{ cm}.$ 

Find: (1) The length of  $\overline{BC}$  (2) m ( $\angle$  BAD)



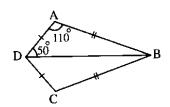
(8) In the opposite figure:

BA = BC, DA = DC,

 $m (\angle ADB) = 50^{\circ}$  and

 $m (\angle BAD) = 110^{\circ}$ 

Find: m (∠ ABC)

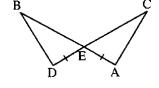


(9) In the opposite figure:

 $\overline{AB} \cap \overline{CD} = \big\{ E \big\}$  , AE = ED and  $\angle \ A \equiv \angle \ D$ 

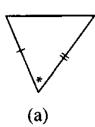
Is  $\triangle$  ACE  $\equiv$   $\triangle$  DBE ? Why ?

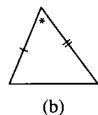
Prove that : CE = EB

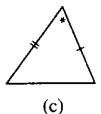


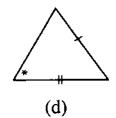
#### [3] Choose the correct answer:

(1) The following triangles are congruent except .......



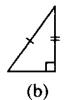




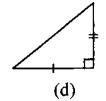


(2) The following triangles are congruent except ......

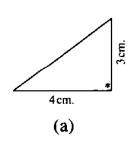


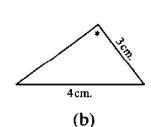


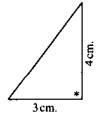




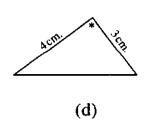
(3) The following triangles are congruent except .......







(c)



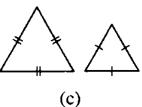
(4) The pair of congruent triangles of the following triangles is ........

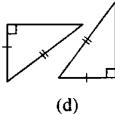










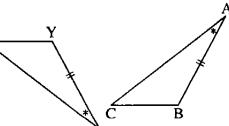


(5) In the opposite figure:

(a)

The necessary and enough condition which makes the two triangles ABC and XYZ be congruent is .........





- (a) BC = YZ
- (b) AC = XZ
- (c) m ( $\angle$  C) = m ( $\angle$  Z)
- (d) m ( $\angle$  B) = m ( $\angle$  Z)



#### [4] Complete the following:

- (1) If:  $\triangle$  ABC  $\equiv$   $\triangle$  XYZ, m ( $\angle$  A) = 50° and m ( $\angle$  B) = 60°, then: m ( $\angle$  Z) = .......°
- (2) If:  $\triangle$  ABC  $\equiv$   $\triangle$  LMN, m ( $\angle$  L) = 40° and m ( $\angle$  B) = 90°, then: m ( $\angle$  C) = .......°
- (3) If:  $\triangle$  ABC  $\equiv$   $\triangle$  XYZ and m ( $\angle$  A) + m ( $\angle$  B) = 120°, then: m ( $\angle$  Z) = .......°
- (4) If:  $\triangle$  ABC  $\equiv$   $\triangle$  DEF and m ( $\angle$  C) = 90°, then: m ( $\angle$  D) + m ( $\angle$  E) = .......°
- (5) If:  $\triangle$  ABC  $\equiv$   $\triangle$  XYZ, the perimeter of  $\triangle$  ABC = 12 cm., XY = 4 cm. and YZ = 5 cm., then: AC = ........
- (6) Any two triangles are congruent if each ...... is congruent to its corresponding side in the other triangle.
- (7) Any two triangles are congruent if two angles and ..... in one of the triangles are congruent to their corresponding elements in the other.
- (8) The diagonal of the rectangle divides its surface into two ...... triangles.
- (10) If: AB = LM, BC = MN and  $m (\angle B) = m (\angle M)$ , then the two triangles .......... and ......... will be congruent.



# Sheet (6) Parallelism

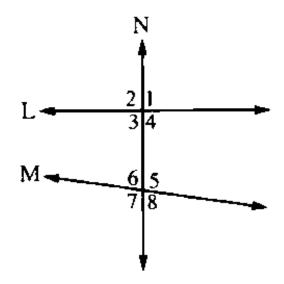
# Angles Formed from two straight lines and a transversal:

If a straight line N cuts two straight lines L and M as shown in the opposite figure, then we get eight angles.

We can classify these angles into pairs of angles:

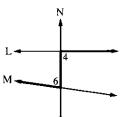


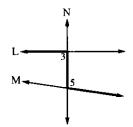
- Corresponding angles.
- Interior angles on the same side of the transversal.



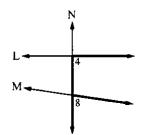
As follows

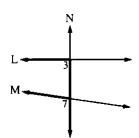
(1) Pairs of alternate angles:

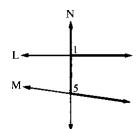


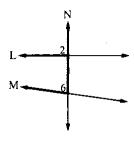


(2) Pairs of corresponding angles:

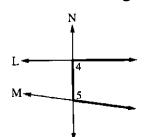


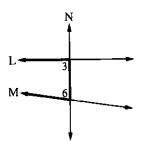






(3) Pairs of interior angles on the same side of the transversal





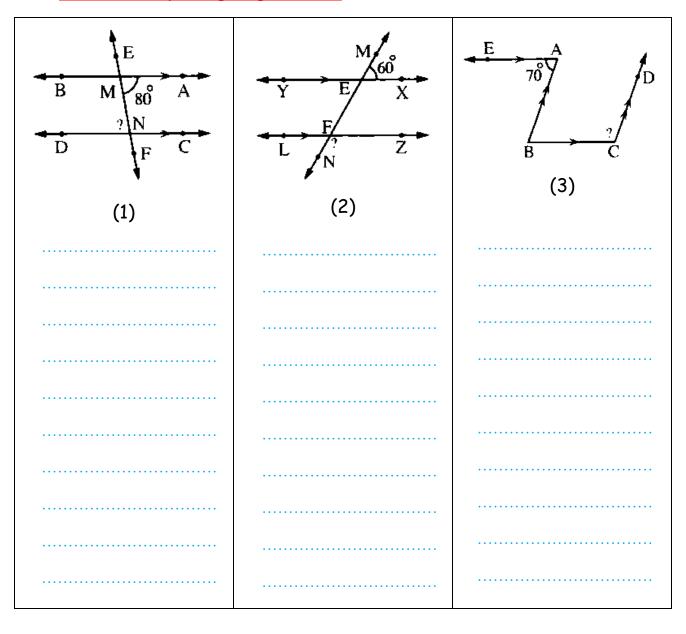
# Relation between pairs of angles formed from two parallel straight lines and a transversal to them

If a straight line intersects two parallel lines, then:

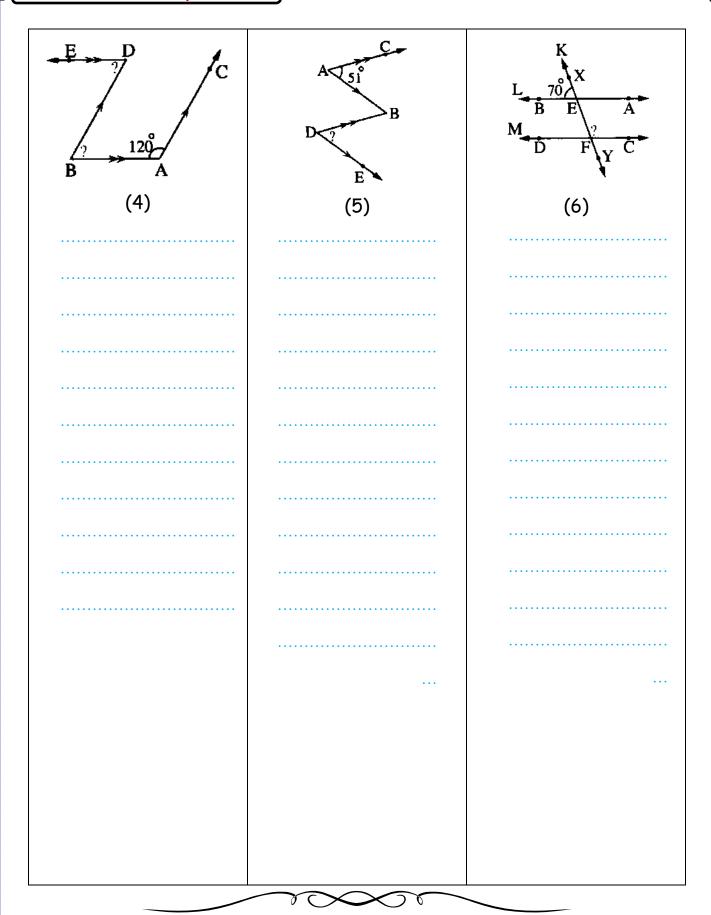
- (1) Each two alternate angles are equal in measure.
- (2) Each two corresponding angles are equal in measure.
- (3) Each two interior angles in the same side of the transversal are supplementary.



In each of the following figures, find the measure of the angle which is marked by (?) giving reason:



# Mathematics 1st Prep 1st term



#### The condition of parallelism of two straight lines

The two straight lines are parallel if a third straight line intersects them (as a transversal) and one of the following cases satisfied:

- (1) Two alternate angles have the same measure.
- (2) Two corresponding angles have the same measure.
- (3) Two interior angles in the same side of the transversal are supplementary.



In each of the following figures, why is  $\overrightarrow{AB}$  //  $\overrightarrow{CD}$ ?

B A E 52° 52° F C (1)	B E A 126° C (2)	B A E 125° E (3)

#### Geometric facts

- (1) The perpendicular to one of two parallel straight lines is perpendicular to the other.
- (2) If two straight lines are perpendicular to a third one, then the two straight lines are parallel.
- (3) If two straight lines are parallel to a third one, then the two straight lines are parallel.
- (4) If parallel straight lines divide a straight line into segments of equal lengths, then they divide any other line into segments of equal lengths.

If  $L_1$  //  $L_2$  //  $L_3$  //  $L_4$ ,

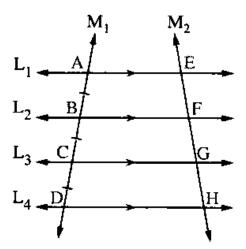
and  $M_1$  and  $M_2$  are two transversal

in which:

$$AB = BC = CD$$
.

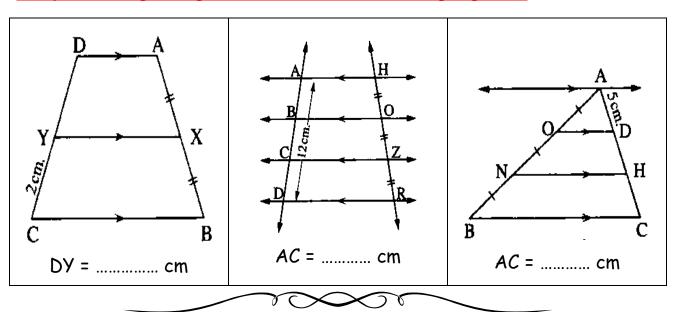
then:

$$EF = FG = GH$$





#### Complete using the given shown in the following figures:



#### [1] Choose the correct answer:

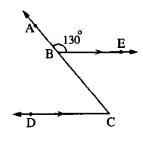
(1) In the opposite figure:

 $B \in \overline{AC}$ ,  $\overrightarrow{BE} / / \overrightarrow{CD}$  and m ( $\angle ABE$ ) = 130°

Then m ( $\angle$  C) = ········

- (a) 130°
- (b) 40°
- (c) 50°

(d) 90°



#### (2) In the opposite figure:

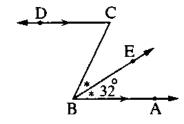
BE bisects  $\angle$  ABC,  $\overrightarrow{BA}$  //  $\overrightarrow{CD}$  and m ( $\angle$  ABE) = 32°, then m ( $\angle$  C) = .........

(a) 32°

(b) 64°

(c) 60°

(d) 80°

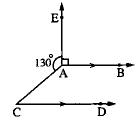


#### (3) In the opposite figure:

 $\overrightarrow{AB}$  //  $\overrightarrow{CD}$ , m ( $\angle$  EAC) = 130° and m ( $\angle$  EAB) = 90°, then m ( $\angle$  C) = .......

(a) 90°

- (b) 130°
- (c) 140°
- (d) 40°



#### (4) In the opposite figure:

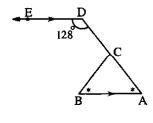
 $\overline{AB}$  //  $\overline{DE}$ , m ( $\angle D$ ) = 128°, m ( $\angle A$ ) = m ( $\angle B$ ) and C  $\in \overline{AD}$ , then m ( $\angle B$ ) = ........

(a) 64°

(b) 128°

(c) 52°

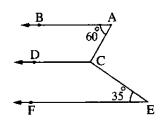
(d) 26°



(5) In the opposite figure:

 $\overrightarrow{AB}$  //  $\overrightarrow{CD}$ ,  $\overrightarrow{AB}$  //  $\overrightarrow{EF}$ , m ( $\angle A$ ) = 60° and m ( $\angle E$ ) = 35°, then m ( $\angle ACE$ ) = .......

- (a) 60°
- $(b) 35^{\circ}$
- (c) 95°
- (d) 85°



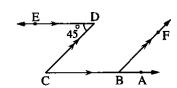
(6) In the opposite figure:

m ( $\angle$  D) = 45°,  $\overrightarrow{DE}$  //  $\overrightarrow{CA}$  and

 $\overrightarrow{CD} / / \overrightarrow{BF}$ , then m ( $\angle ABF$ ) = ......

(a)  $45^{\circ}$ 

- (b) 90°
- (c) 135°
- (d) 40°



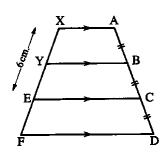
(7) In the opposite figure:

$$\overline{AX} // \overline{BY} // \overline{CE} // \overline{DF}$$

$$AB = BC = CD$$

and 
$$XE = 6$$
 cm.

- then the length of  $\overline{YF} = \cdots$
- (a) 3 cm.
- (b) 6 cm.
- (c) 12 cm.
- (d) 9 cm.



#### (8) In the opposite figure:

$$\overrightarrow{AB} / \overrightarrow{CF} / \overrightarrow{DE}$$
,

$$m (\angle A) = 120^{\circ} \text{ and } m (\angle D) = 85^{\circ}$$
,

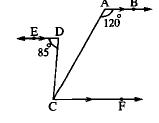
then m ( $\angle$  ACD) = ········

(a) 60°

(b) 85°

 $(c) 25^{\circ}$ 

(d) 120°



#### (9) In the opposite figure:

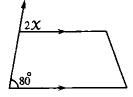
What is the value of X?

(a)  $40^{\circ}$ 

(b) 60°

(c) 80°

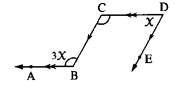
(d) 100°



#### (10) In the opposite figure:

- then :  $x = \cdots$
- (a)  $60^{\circ}$

- (b)  $45^{\circ}$
- (c) 120°
- (d) 90°



#### [2] Complete:

- (1) The straight line which is perpendicular to one of two parallel straight lines is ...... to the other straight line in the plane.
- (2) If two straight lines are parallel to a third straight line, then they are ........
- (3) If a straight line cuts two parallel straight lines, then each two alternate angles are ........
- (4) If a straight line cuts two parallel straight lines, then each two corresponding angles are ........

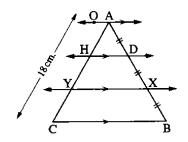
- (5) If a straight line cuts two parallel straight lines, then each two interior angles in the same side of the transversal are ........
- (6) If a straight line cuts two straight lines and there are two corresponding angles having the same measure, then the two straight lines are .........
- (7) If a straight line cuts two straight lines and there are two alternate angles having the same measure, then the two straight lines are .........
- (8) If a straight line cuts two straight lines and there are two interior angles in the same side of the transversal are supplementary, then the two straight lines are ........
- (9) If a straight line cuts several parallel lines and the intercepted parts of this transversal between these parallel straight lines are equal in length, then the intercepted parts for any transversal are ........



#### [3] Answer the following:

(1) In the opposite figure:  $\overrightarrow{AO} // \overrightarrow{HD} // \overrightarrow{YX} // \overrightarrow{CB}$   $\overrightarrow{AO} = DX = XB$ and AC = 18 cm.

Find the length of  $\overline{AY}$ 



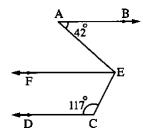
	• • • • • • • • • • • • • • • • • • • •	

(2) In the opposite figure:

 $\overrightarrow{AB} / / \overrightarrow{CD}, \overrightarrow{EF} / / \overrightarrow{CD}$ 

, m ( $\angle$  A) = 42° and m ( $\angle$  C) = 117°

**Determine:** m (∠ AEC)

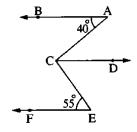


(3) In the opposite figure:

$$m (\angle A) = 40^{\circ}, m (\angle E) = 55^{\circ}$$

 $\overrightarrow{AB}$  //  $\overrightarrow{EF}$  and  $\overrightarrow{AB}$  //  $\overrightarrow{CD}$ 

**Find**:  $m (\angle ACE)$ 



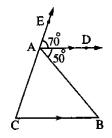
<b>Mathematics</b>	1 <sup>st</sup>	Prep	1 <sup>st</sup>	term
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(4) In the opposite figure:

 $\overrightarrow{AD} / / \overrightarrow{BC}$ ,  $E \in \overrightarrow{CA}$ ,

m ( $\angle$  DAE) = 70° and m ( $\angle$  DAB) = 50°

Find the measures of the triangle ABC

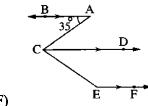


(5) In the opposite figure:

 $\overrightarrow{AB} / / \overrightarrow{CD} / / \overrightarrow{EF}$ , m ( $\angle A$ ) = 35° and

 $\overrightarrow{CD}$  bisects  $\angle$  ACE

Find: (1) m ( $\angle$  DCE)



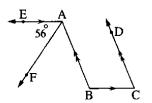
(2) m ( $\angle$  CEF)

(6) In the opposite figure:

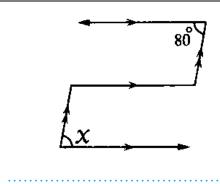
 $\overrightarrow{AE} // \overrightarrow{CB}, \overrightarrow{BA} // \overrightarrow{CD},$ 

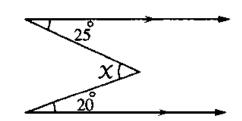
 $\overrightarrow{AF}$  bisects  $\angle$  BAE and m ( $\angle$  EAF) = 56°

Find:  $m (\angle C)$ 



[4] Find the value of x:





105° X	35° X
	<i>•</i>

# 4-4 Congruent 4rlangles

# The cases of congruence of two triangles

Two sides and the included angle

Two angles and one side

Three sides

Hypotenuse and one side in the rightangled triangle

#### **EXAMPLE:**

In each of the following figures, show if the two triangles are congruent or not.

If they are congruent, name the case of congruence. If they are not congruent, give reason (Given that the similar signs denote the congruency of the elements marked by these signs).



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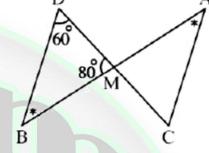
#### **EXAMPLE:**

7) In the opposite figure:

 $\overline{AB} \cap \overline{CD} = \{M\}$ , M is the midpoint of  $\overline{AB}$ ,

$$m (\angle A) = m (\angle B) \cdot m (\angle D) = 60^{\circ}$$

and m ( $\angle$  DMB) =  $80^{\circ}$ 



Find:  $m (\angle C)$  with showing the steps of the solutions.





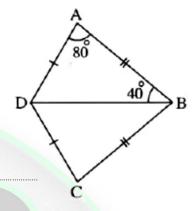


8) In the opposite figure:

$$BA = BC \cdot DA = DC \cdot$$

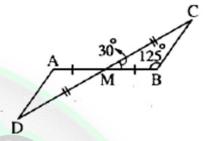
$$m (\angle ABD) = 40^{\circ} \text{ and } m (\angle BAD) = 80^{\circ}$$

Find:  $m (\angle ADC)$  with showing the steps of the solution.

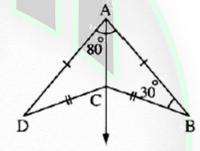


### In each of the following figures, find the required under each figure:

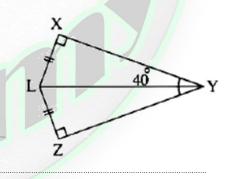
9)  $\overline{AB} \cap \overline{CD} = \{M\} \text{ m } (\angle D) = \cdots$ 



10) m (∠D) = ········° , m (∠BAC) = ·········°



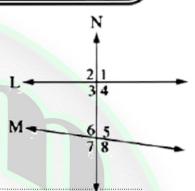
11) m (\(\angle XLY\) = \(\dots\)



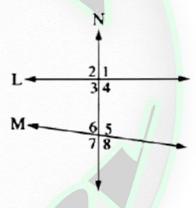
### 4-5 Parallelism

## Angles formed from two straight lines and a transversal :

Pairs of alternate angles :



Pairs of corresponding angles :



3 Pairs of interior angles on the same side of the transve

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M-	6 5 7 8	_
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Relation between pairs of angles formed from two parallel straight lines and a transversal to them :

If a straight line intersects two parallel straight lines, then each two alternate angles are equal in measure.

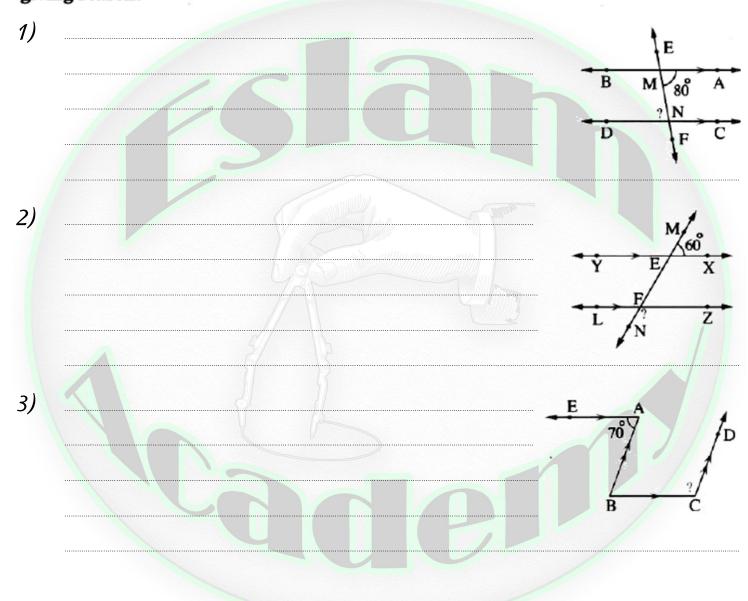
If a straight line intersects two parallel straight lines, then each two corresponding angles are equal in measure.

If a straight line intersects two parallel straight lines, then each two interior angles in the same side of the transversal are supplementary.

$\frac{A > \frac{2}{3} \sqrt{4}}{4}$	B
$\frac{6 \setminus 5}{C}$	Ď
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#### **EXAMPLE:**

In each of the following figures, find the measure of the angle which is marked by "?" giving reason.

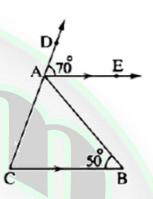


#### **EXAMPLE:**

4) In the opposite figure :  $\overrightarrow{AE} /\!/ \overrightarrow{BC}$ ,  $D \in \overrightarrow{CA}$ ,  $m (\angle DAE) = 70^{\circ}$  and

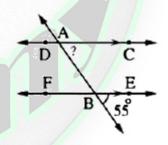
 $m (\angle B) = 50^{\circ}$  Find giving reason:

 $1 m (\angle EAB) 2 m (\angle C) 3 m (\angle EAC)$ 

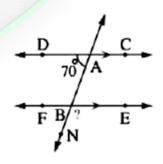


In each of the following figures, find the measure of the angle which is written under each figure (giving reason):

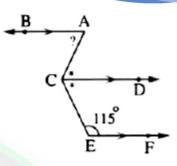
5) m (∠ CAB) = ······· The reason is -



*6)* m (∠ EBN) = ...... The reason is ......



7)  $m (\angle A) = \cdots ^{\circ}$ The reason is .......



# EXAMPLE: In each of the following, show why $\overrightarrow{AB}$ is parallel to $\overrightarrow{CD}$

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#### From the previous, we deduce that:

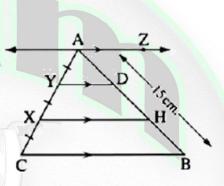
If parallel straight lines divide a straight line into segments of equal lengths, then they divide any other straight line into segments of equal lengths.

#### **EXAMPLE:**

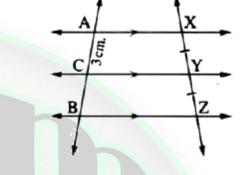
11) In the opposite figure:

$$AY = YX = XC$$
 and  $AB = 15$  cm.

Find the length of BD showing the reason.



### Complete under each figure of the following figures:



13) BH = ..... cm. The perimeter of  $\triangle$  ADY = ..... cm.

